



National Research
Council of Italy



NDlib: a Python Library to Model and Analyze Diffusion Processes Over Complex Networks

IEEE DSAA 2018
Turin, Italy
1-4 October, 2018

Letizia Milli, Giulio Rossetti, Salvatore Rinzivillo
{name.surname}@isti.cnr.it





Horizon 2020, EU Projects

NDlib is funded by the European Community's H2020 Program



Founding Scheme:

“FETPROACT-1- 2014: Global Systems Science (GSS)”

Project:

CIMPLEX, Bringing Citizens, Models and Data together in Participatory, Interactive Social EXploratories

Website:

<https://www.cimplex-project.eu>



Founding Scheme:

“INFRAIA-1-2014-2015: Research Infrastructures”

Project:

SoBigData, Social Mining & Big Data Ecosystem

Website:

<http://www.sobigdata.eu>



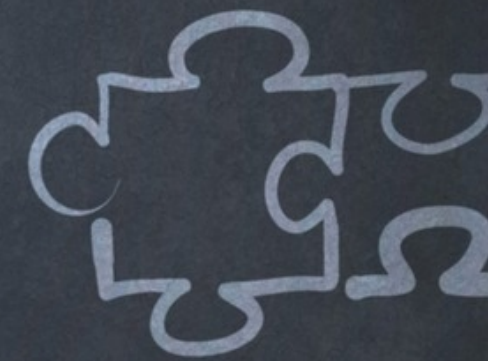


Strategy Innovation



Vision
Creativity

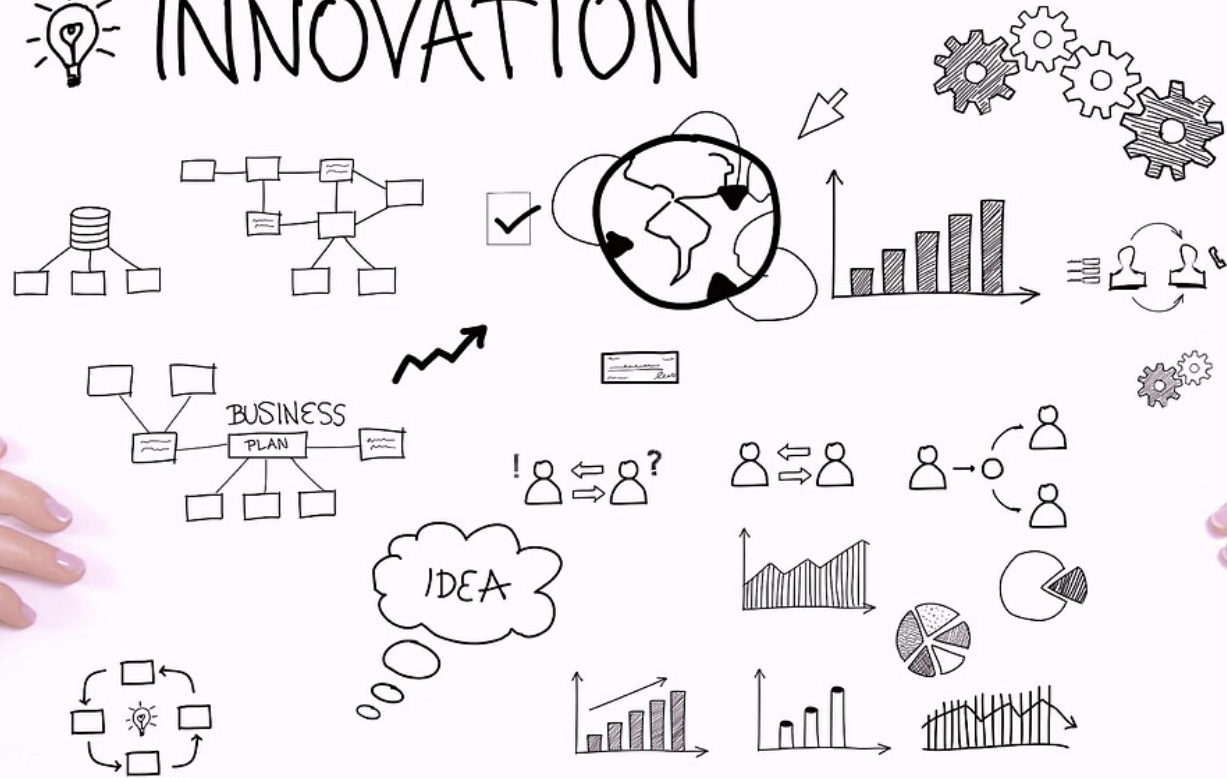
Support



Solution



INNOVATION





Why do diffusive processes matter now?

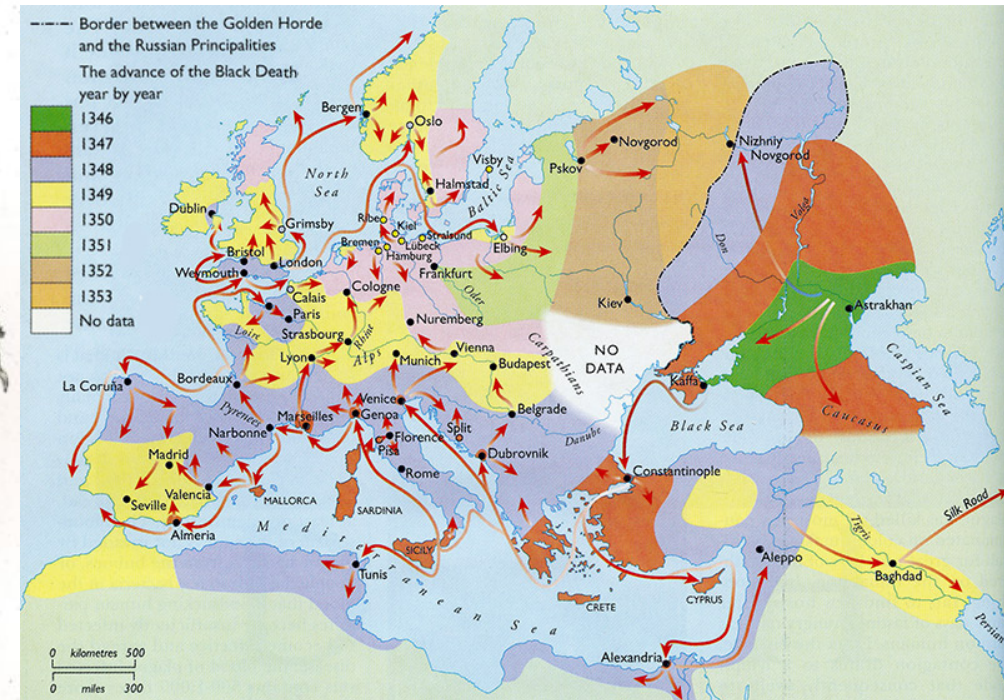
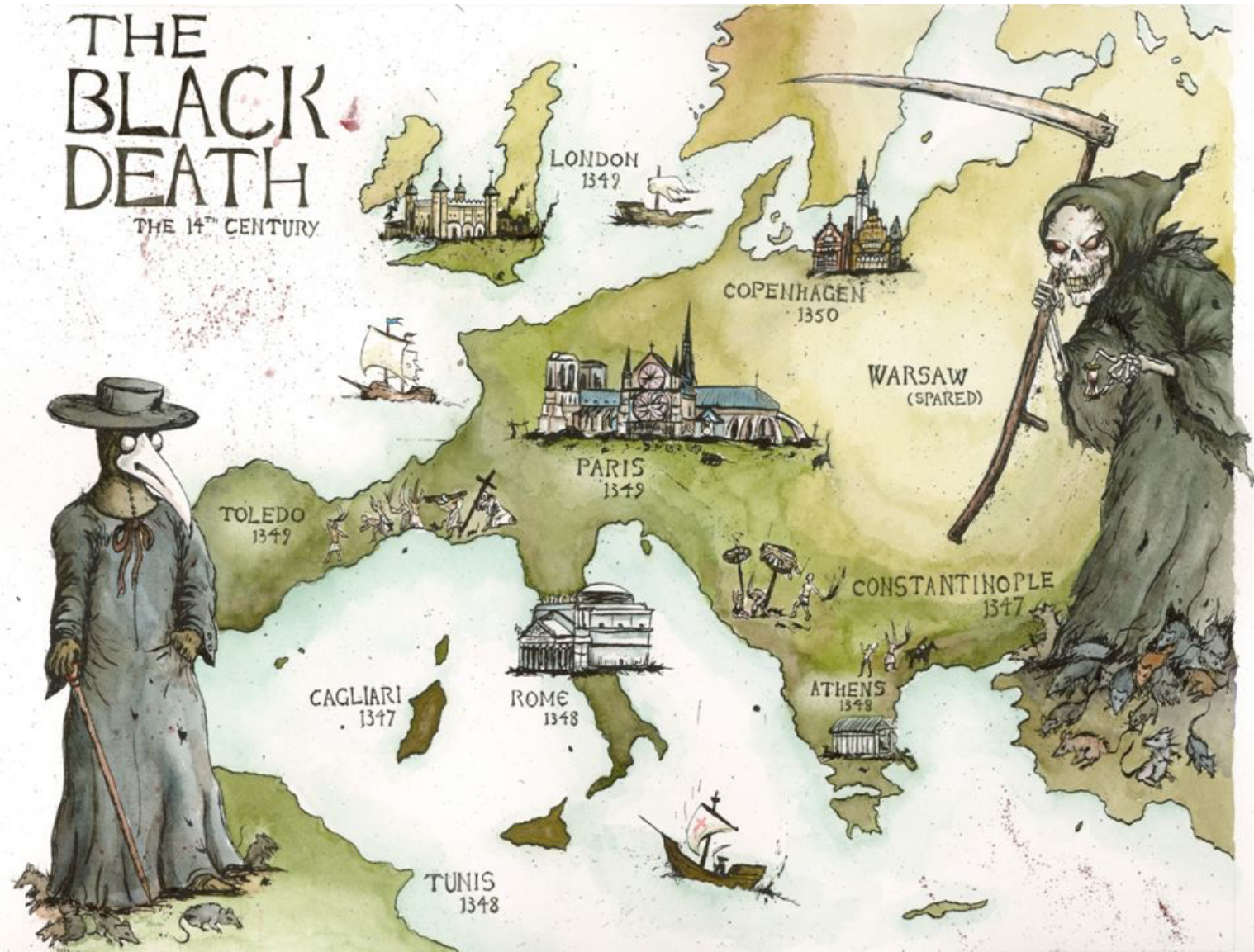


High mobility

High population density



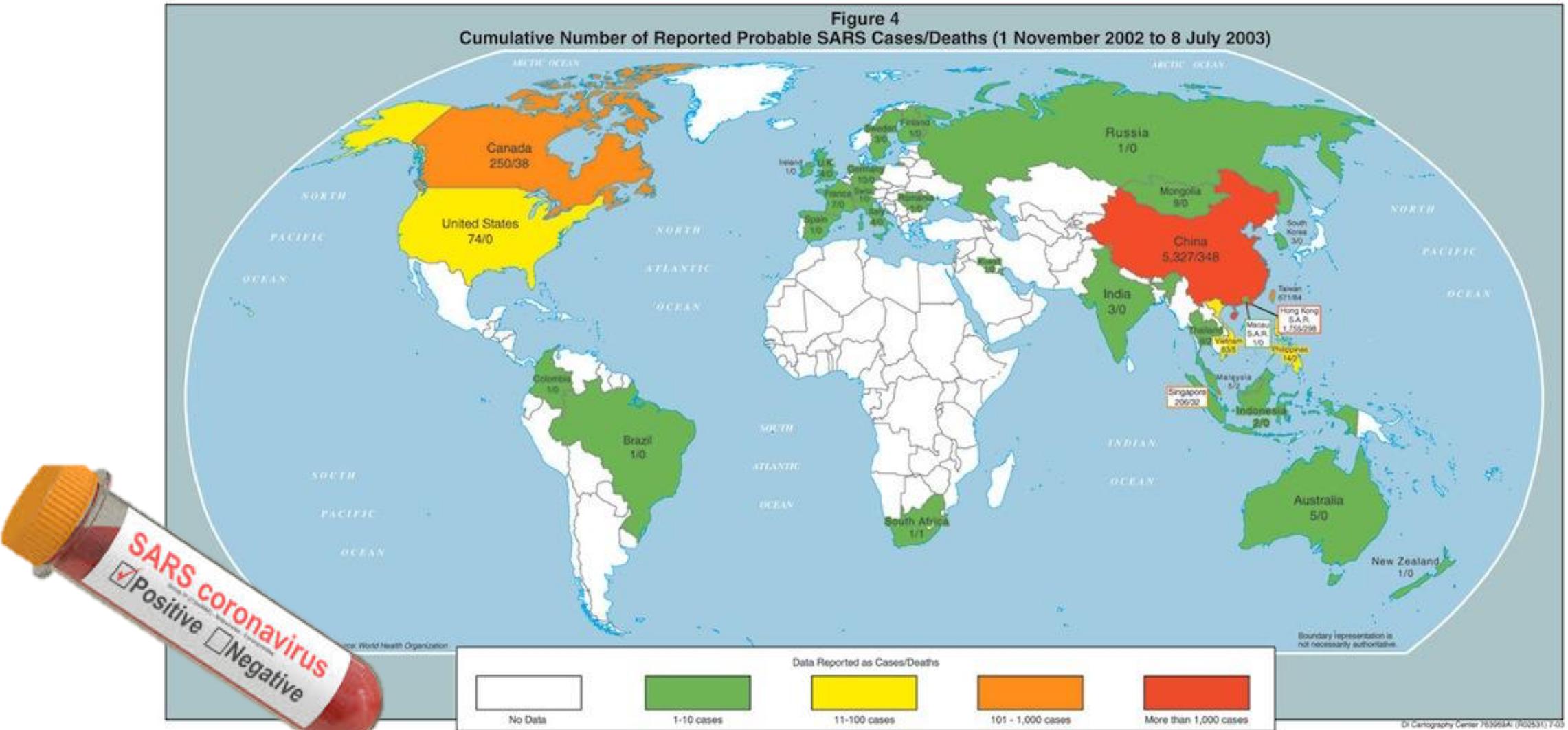
The great plague in 14th century



4 years from France to Sweden

SARS in 21th century

6 months...

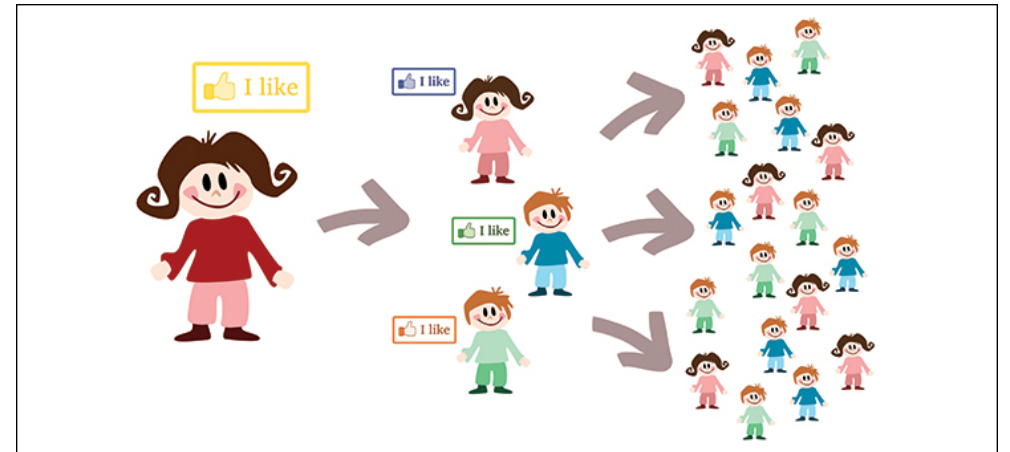


Epidemics, Opinions, Innovations...



The difference: the degree of *activeness* of the subjects they affect

- Passive: viruses...
- Active: ideas, adoptions...



$|F_n| = mg \cos \theta$; $\sum F_x = \max$
 $M_R, L = \frac{mg \sin \theta \cdot \max}{mg \cos \theta \cdot \max} = \tan \theta \cdot \max$
 $F_{R, \max} = -m g \sin \theta \cdot \max = 0$
 $= -mg \sin \theta \cdot \max$

$E_{\text{mech}, A} = 0$
 $E_{\text{mech}, B} = E_{\text{mech}, A}$
 $\frac{1}{2} m v_0^2 + m g y_0 = \frac{1}{2} m v_1^2 + m g y_1$
 $\frac{1}{2} m v_0^2 = m g h$

$F = m_2 g + 2 P_3$
 $a = \frac{dv}{dt} = \frac{dv}{du} \frac{du}{db}$
 $= \frac{(m_2 - m_1) g}{(m_1 + m_2)}$
 $v = \sqrt{\frac{2(m_2 - m_1) g h}{(m_1 + m_2)}}$

$v = \frac{v}{T} = v \lambda$
 $\omega = k v$
 $\sum F_y = m a_y = F_{\text{oy}} + F_y$
 $= F_{\text{oy}} + F_y$
 $k = \frac{2\pi}{\lambda}$
 $y(x) = A \sin(2\pi \frac{x}{\lambda} + \delta)$
 $y(x) = A \sin(kx - \omega t)$
 $2\pi v = k \lambda = \frac{2\pi}{\lambda} v$
 $\lambda_{\text{max}} = \frac{2.99 \text{ mm} \cdot \text{K}}{T}$
 $P_e = e \sigma A T^4$
 $P_a = e \sigma A T_0^4$
 $\Delta P = e \sigma A (T^4 - T_0^4)$
 $U = F_e r = F \sin \theta = F l$
 $F_{n,x} + F_{a,x} = m a_x$
 $F_{n,x} = 0; F_{a,x} = mg \sin \theta$
 $a_x = g \sin \theta$
 $v^2 = 2 g \sin \theta \Delta x; v^2 = 2 g h$
 $\mu = \chi \log \frac{k_2}{\mu_0}$
 $\oint E \cdot dl = - \frac{d}{dt} \int \Delta n dt$
 $\nabla \cdot B = 0$

$\psi = 0, d = n \frac{2\pi}{\lambda}, n = 1, 2, 3$
 $E = \frac{1}{2} m v^2 = \frac{h^2}{2m}; E_n = \frac{h^2}{2m}$
 $n=4, E_4 = 16 E_1 = \frac{h^2}{2m d^2}$
 $n=3, E_3 = 9 E_1$
 $n=2, E_2 = 4 E_1$
 $n=1, E_1 = E_1$

$|k| = \frac{1}{v \lambda} \frac{d\lambda}{dr}$
 $= \frac{\lambda}{4\pi r}$
 $d\lambda = \lambda \frac{dr}{r}$
 $d\lambda = \frac{2}{4\pi r} \frac{dx}{r} = \frac{2}{4\pi r} \frac{y dr}{r^2}$
 $= \frac{2}{4\pi r} \frac{y dr}{r^2}$

$E_n = n^2 \frac{h^2}{8 m d^2} = n^2 E_1$
 $E_1 = \frac{h^2}{8 m d^2}$
 $v = k_e - E_1$
 $\psi(x,0) = A \exp(-\frac{x^2}{2\sigma^2}) e^{i k x}$

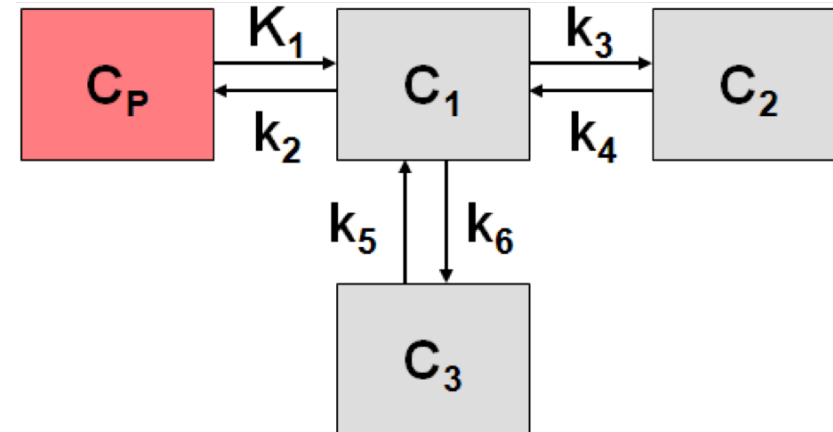
How can we model diffusive phenomena?

Compartmental Models

[Kermack & McKendrick, 1927]

The framework is based on two hypotheses:

1. **Compartmentalization:** each individual is classified into distinct states. The simplest classification assumes that an individual can be in one of the states.
2. **Homogeneous Mixing:** each individual has the same chance of coming into contact with an infected individual.

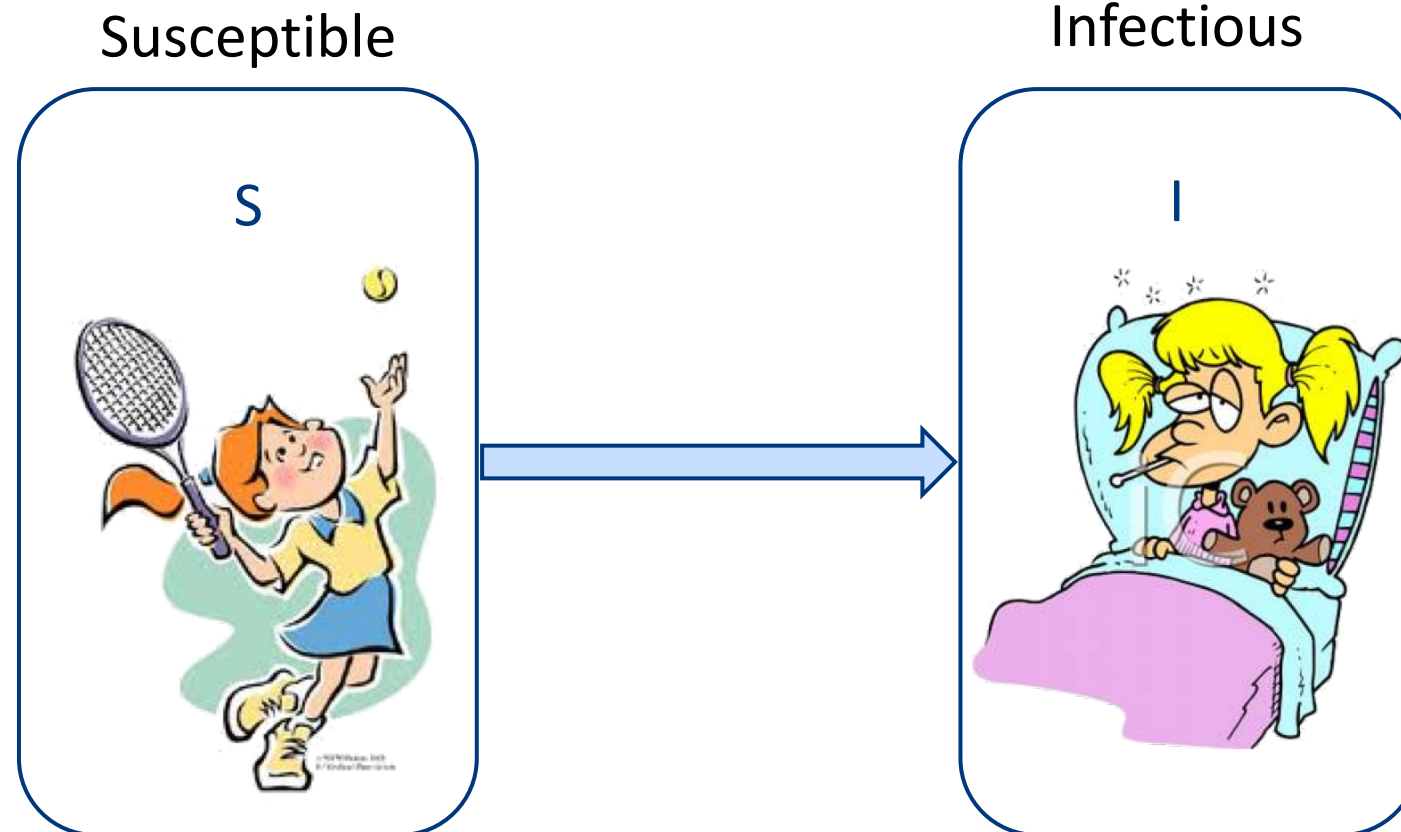


[1927] W. O. Kermack and Ag McKendrick. *A Contribution to the Mathematical Theory of Epidemics*

Compartmental Models

[Kermack & McKendrick, 1927]

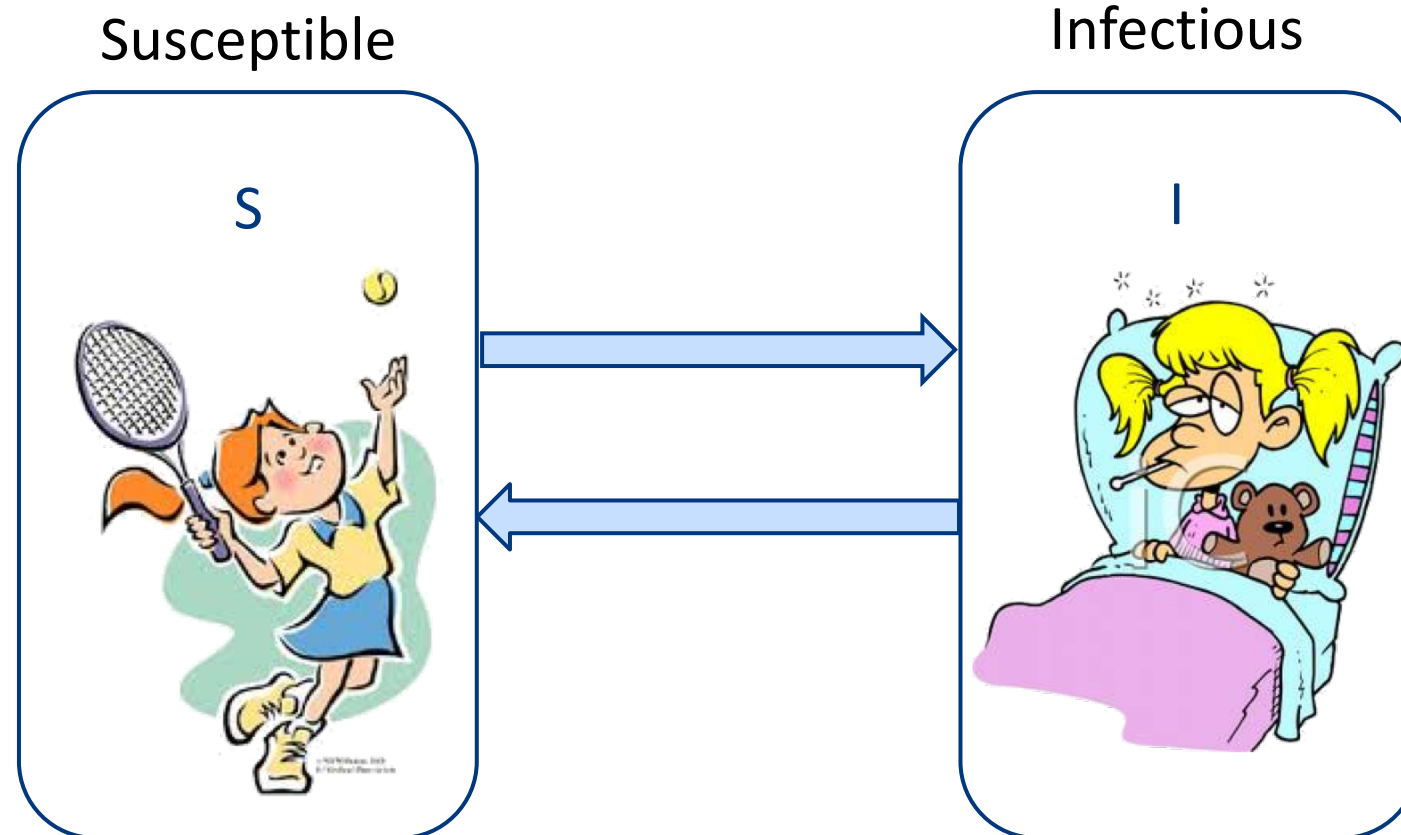
SI MODEL



Compartmental Models

[Kermack & McKendrick, 1927]

SIS MODEL: for common cold



Compartmental Models

[Kermack & McKendrick, 1927]

SIR MODEL

Susceptible



Infectious



Removed



Compartmental Models - Limits

[Kermack & McKendrick, 1927]

It does not take into account:

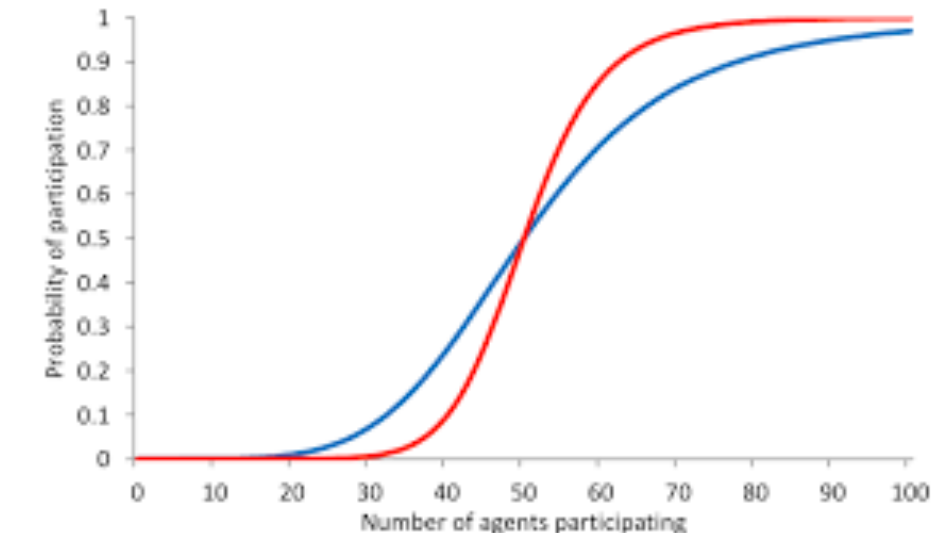
- **Social structure** (i.e., mean field scenario)
- Heterogenous mixing
 - An individual comes into contact only with a restricted set of peers



Threshold Models

[Granovetter, '78]

- Model for:
 - Riots, protests
 - Neighborhoods in cities changing ethnic composition
- Each person i has a threshold t_i
- Node i will adopt the behavior \longleftrightarrow at least t_i other people are adopters:
 - small t_i : *early adopter*
 - large t_i : *late adopter*



[1978] M. Granovetter. *Threshold models of collective behavior.*

Threshold Model- Limits

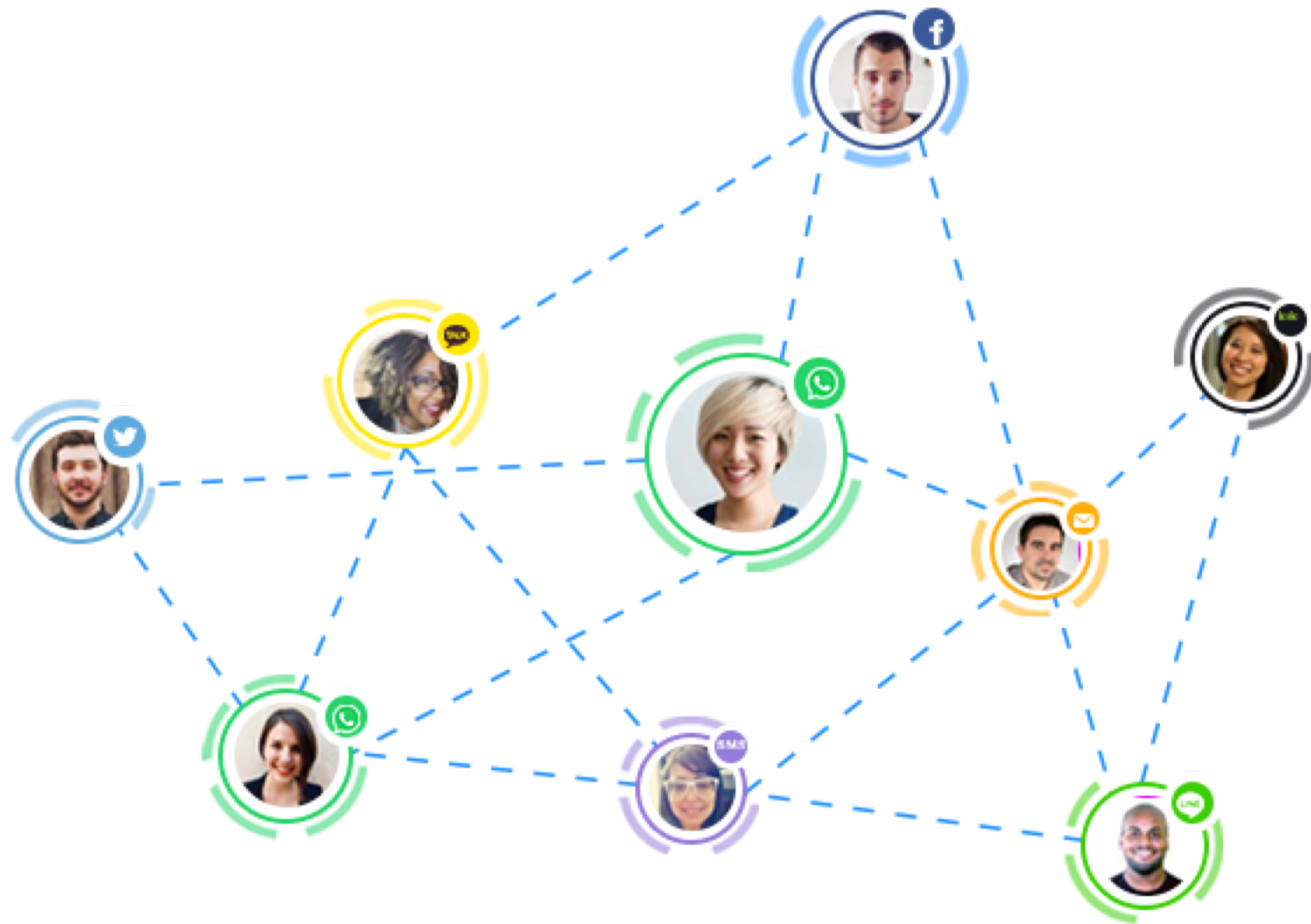
[Granovetter, '78]

It does not take into account:

- **Social structure** (i.e., mean field scenario)
- It matters who the early adopters are, not just how many
- Non monotone behavior – dropping out if too many people adopt
- Modeling thresholds:
 - Richer distributions
 - Deriving thresholds from more basic assumptions



What about social interactions?



Intro to: Complex Networks



Complex

[adj., v. kuh m-pleks, kom-pleks; n. kom-pleks]
–adjective

1.

composed of many interconnected parts;
compound; composite: a complex highway
system.

2.

characterized by a very complicated or
involved arrangement of parts, units, etc.:
complex machinery.

3.

so complicated or intricate as to be hard to
understand or deal with: a complex problem.

Source:
Dictionary.com

Complexity, a **scientific theory** which asserts that some systems display behavioral phenomena that are completely inexplicable by any conventional analysis of the systems' constituent parts. These phenomena, commonly referred to as **emergent behaviour**, seem to occur in many complex systems involving living organisms, such as a stock market or the human brain.

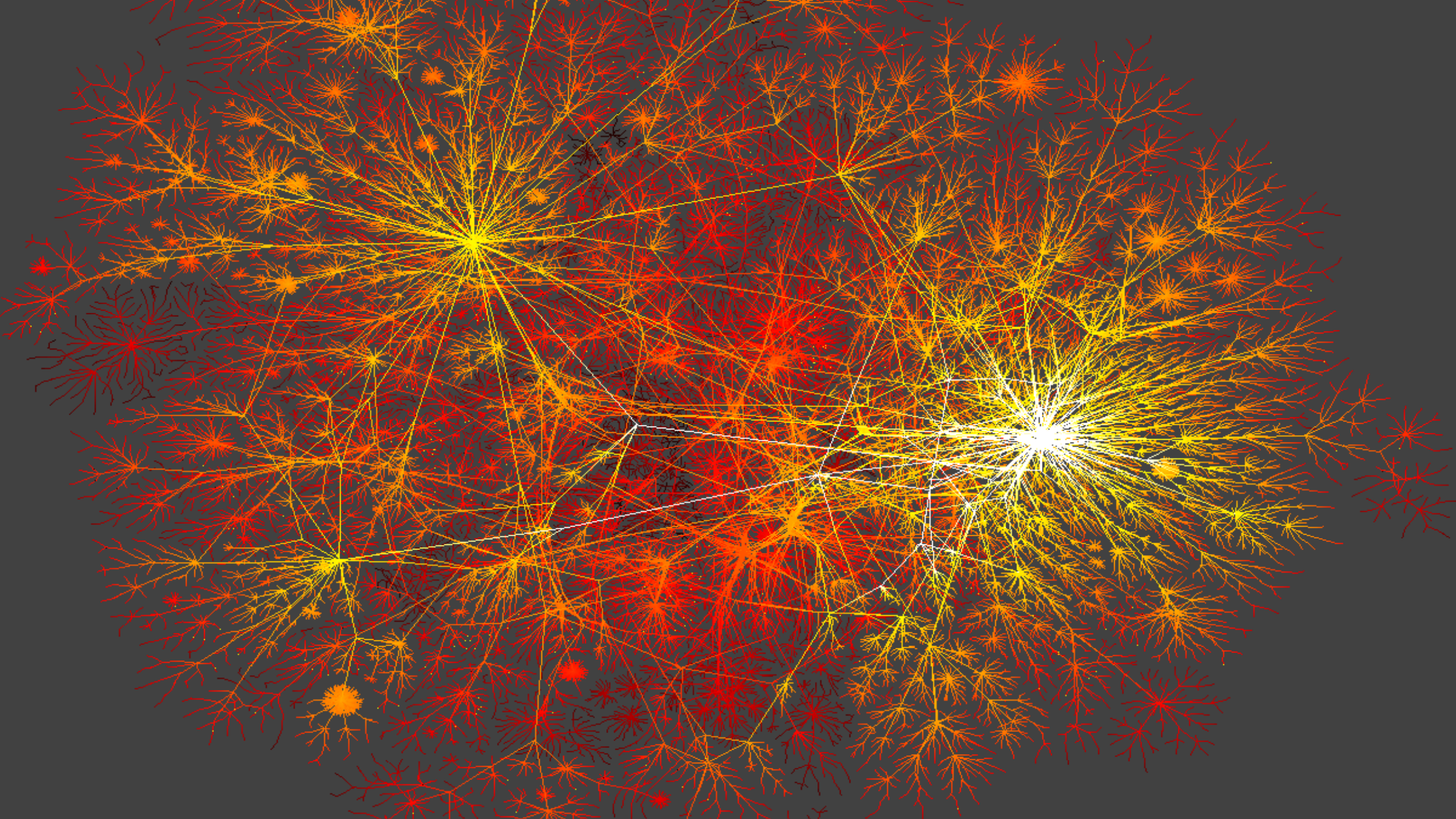
Source: *John L. Casti, Encyclopædia Britannica*

Complexity

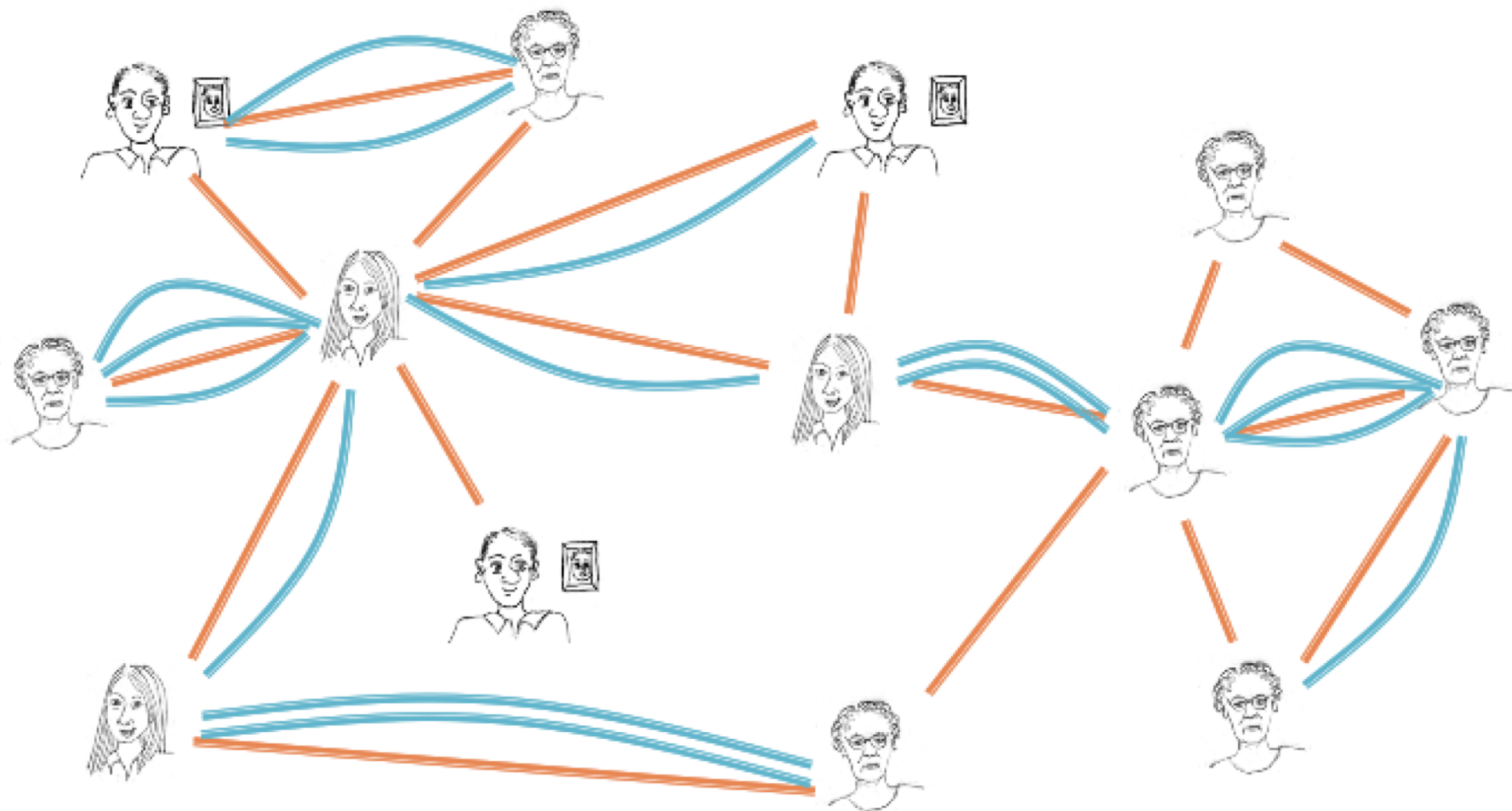
Behind each complex system there is a **network**, that defines the interactions between the components.



Keith Shepherd's "Sunday Best". <http://baseballart.com/2010/07/shades-of-greatness-a-story-that-needed-to-be-told/>

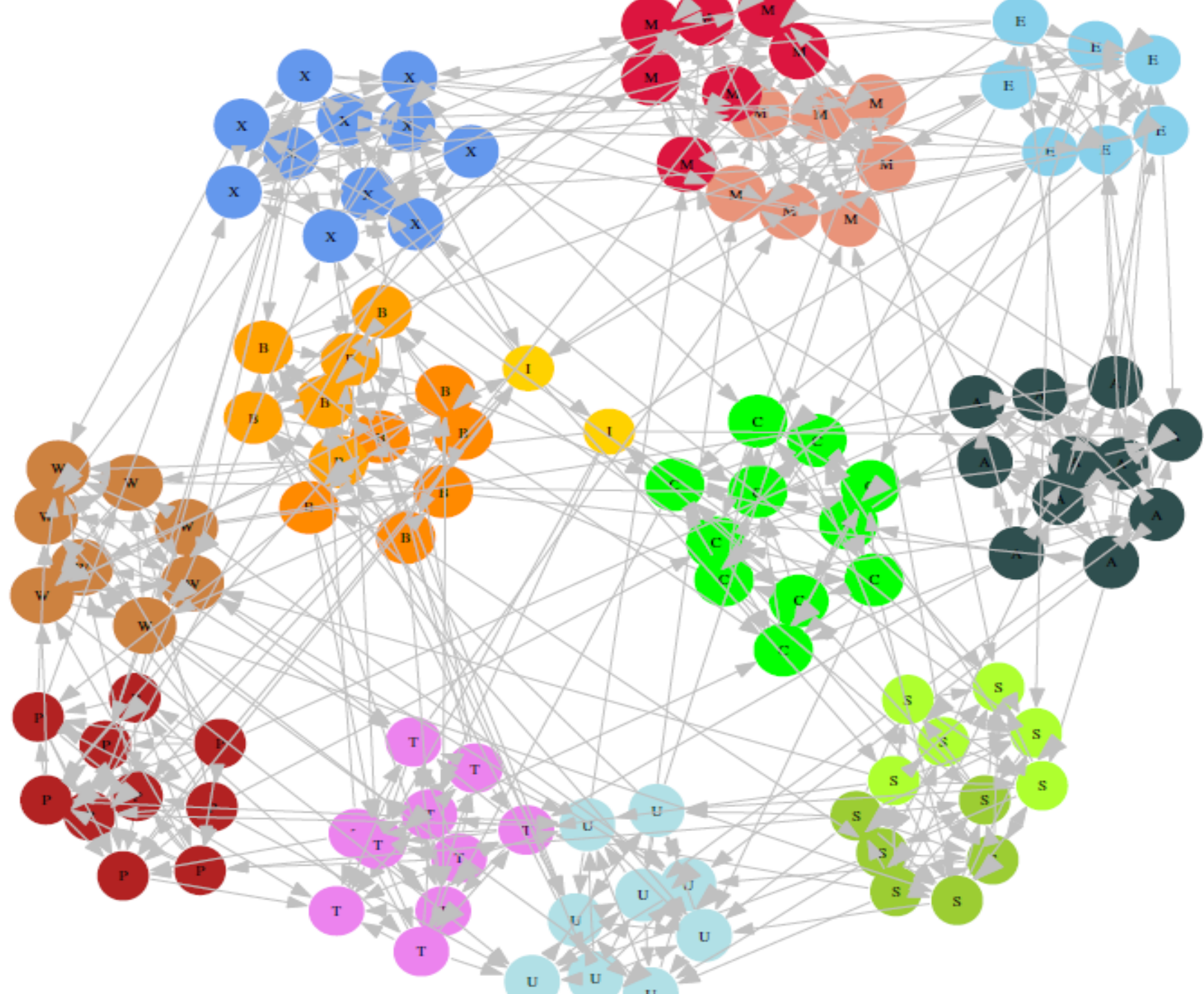




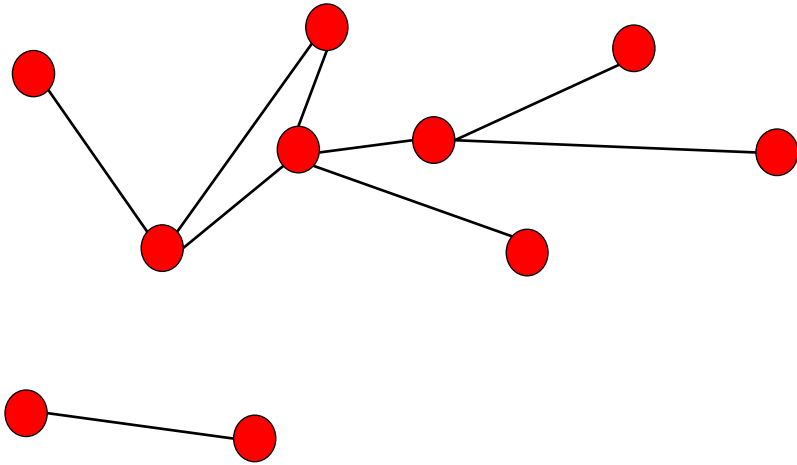


— Buddy

— Conversation



Networks in a nutshell



Network (graph)

a graph $G=(N,L)$ is composed by a set of nodes, N , connected by links, L .

Degree

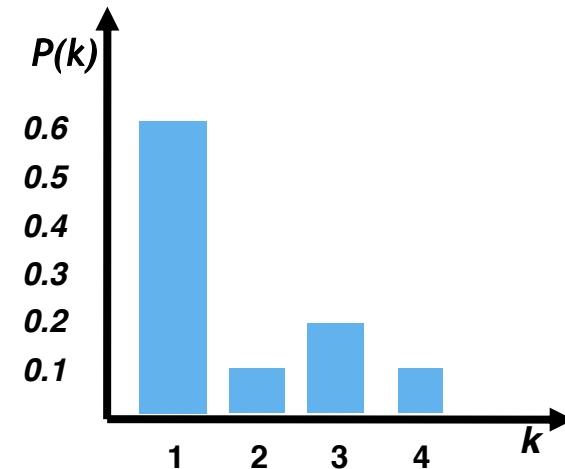
number of links incident to a given node.

Degree distribution

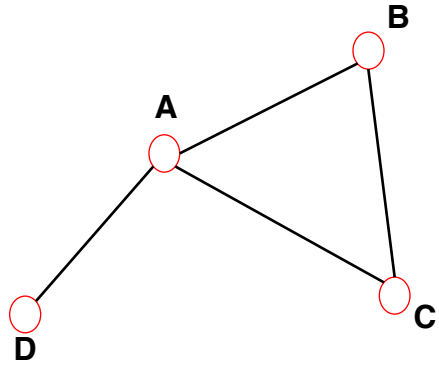
$P(k)$: probability that a randomly chosen vertex has degree k

$N_k = \#$ nodes with degree k

$P(k) = N_k / N \rightarrow$ plot

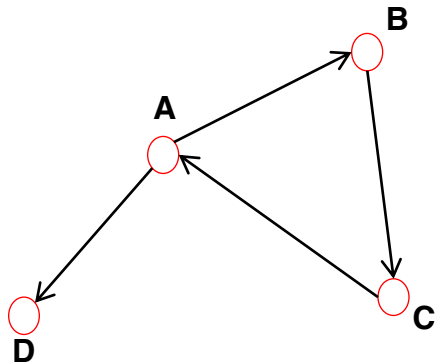


Networks in a nutshell



The *distance (shortest path, geodesic path)* between two nodes is defined as the **number of edges along the shortest path connecting them.**

*If the two nodes are disconnected, the distance is infinity.



In **directed graphs** each path needs to follow the direction of the arrows. Thus in a digraph the distance from node A to B (on an AB path) is generally different from the distance from node B to A (on a BCA path).

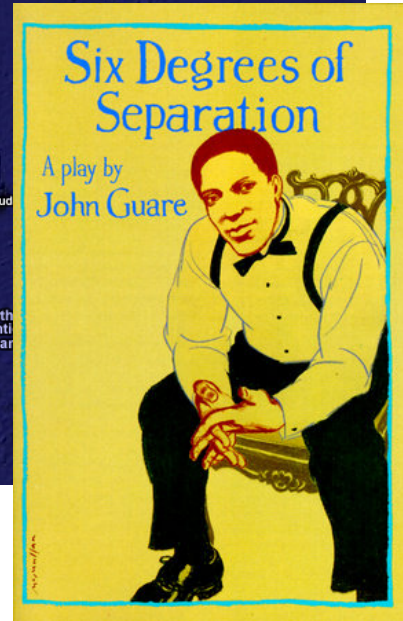
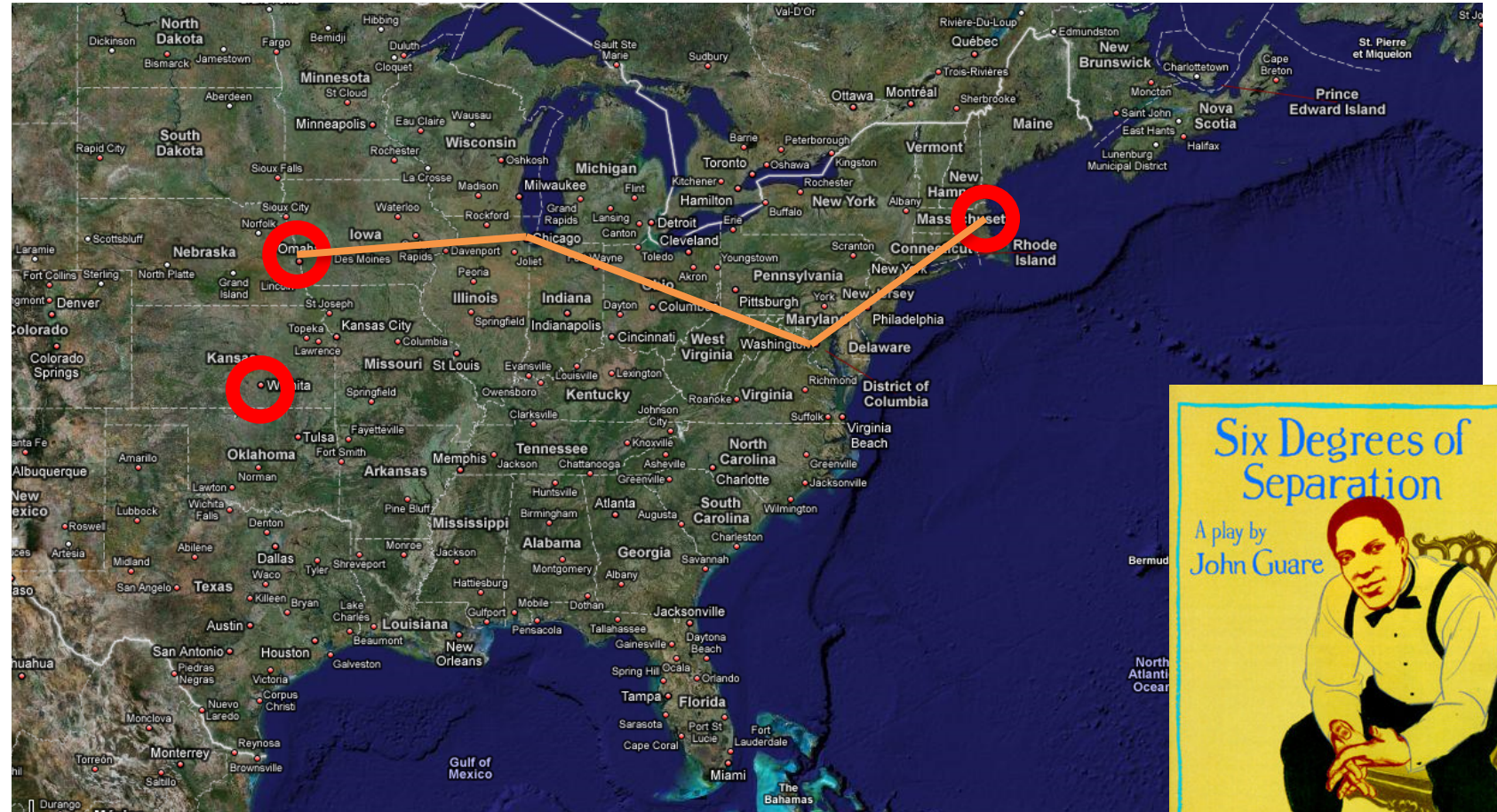
Real world Networks properties: Six Degrees of separation...

“There exist a path of length 6 that connects any 2 nodes in a social graph”

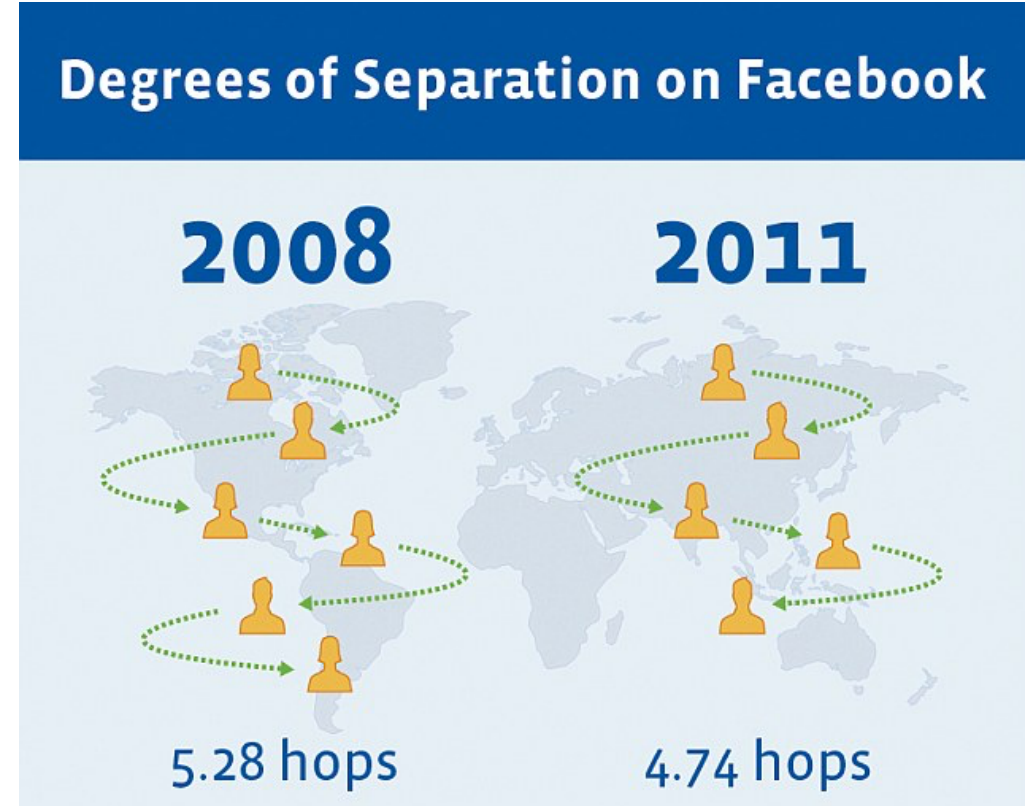
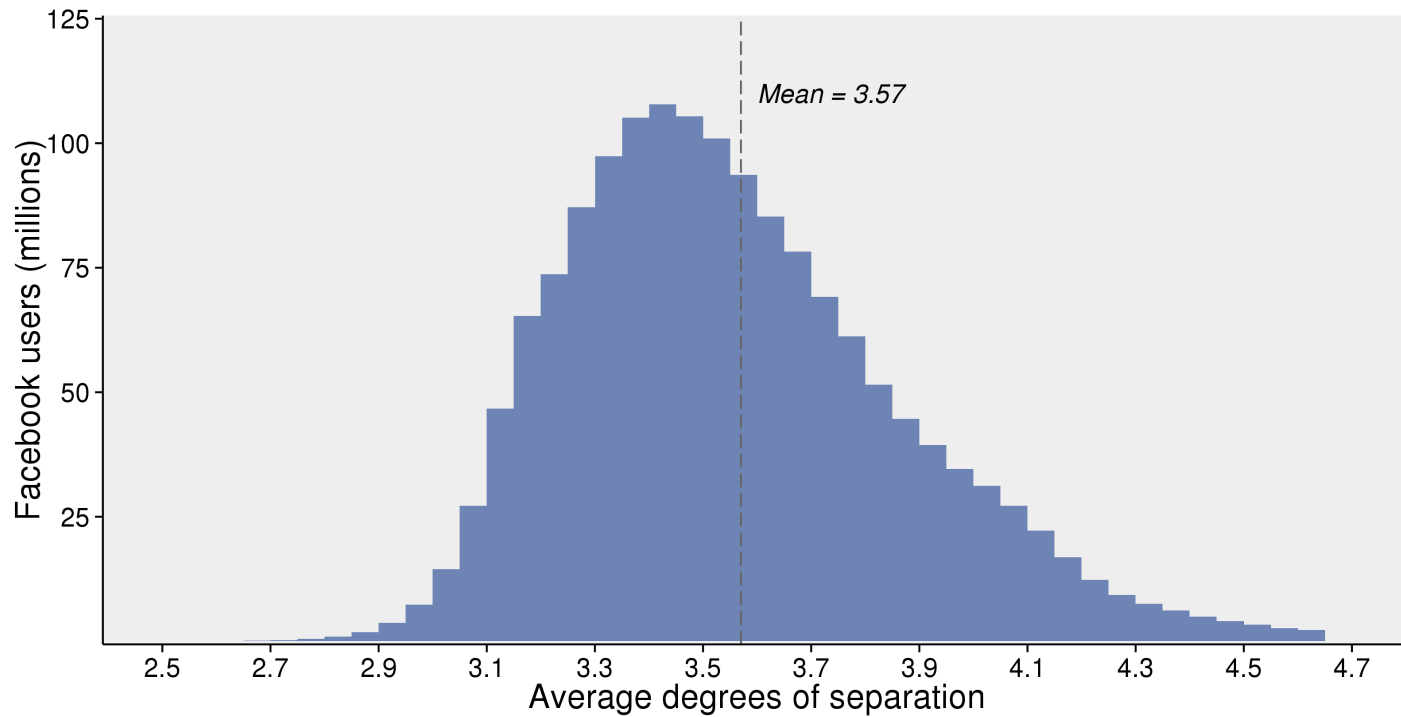
Stanley Milgram



- 160 people in Omaha (Nebraska) & Wichita (Kansas)
- 1 recipient near Boston



... became three (and half) in Facebook

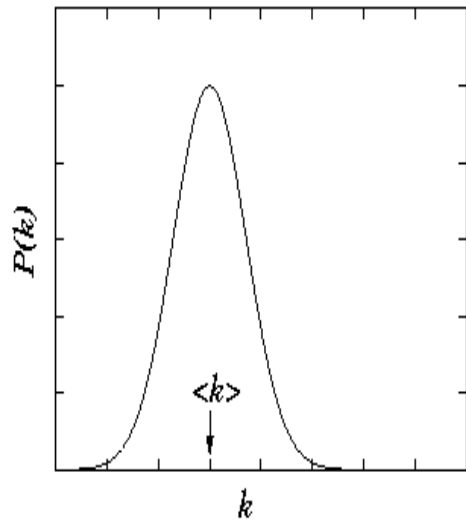


Backstrom, L., Boldi, P., Rosa, M., Ugander, J., & Vigna, S. (2012). [Four degrees of separation](#). *Proceedings of the 4th Annual ACM Web Science Conference*, 33-42.

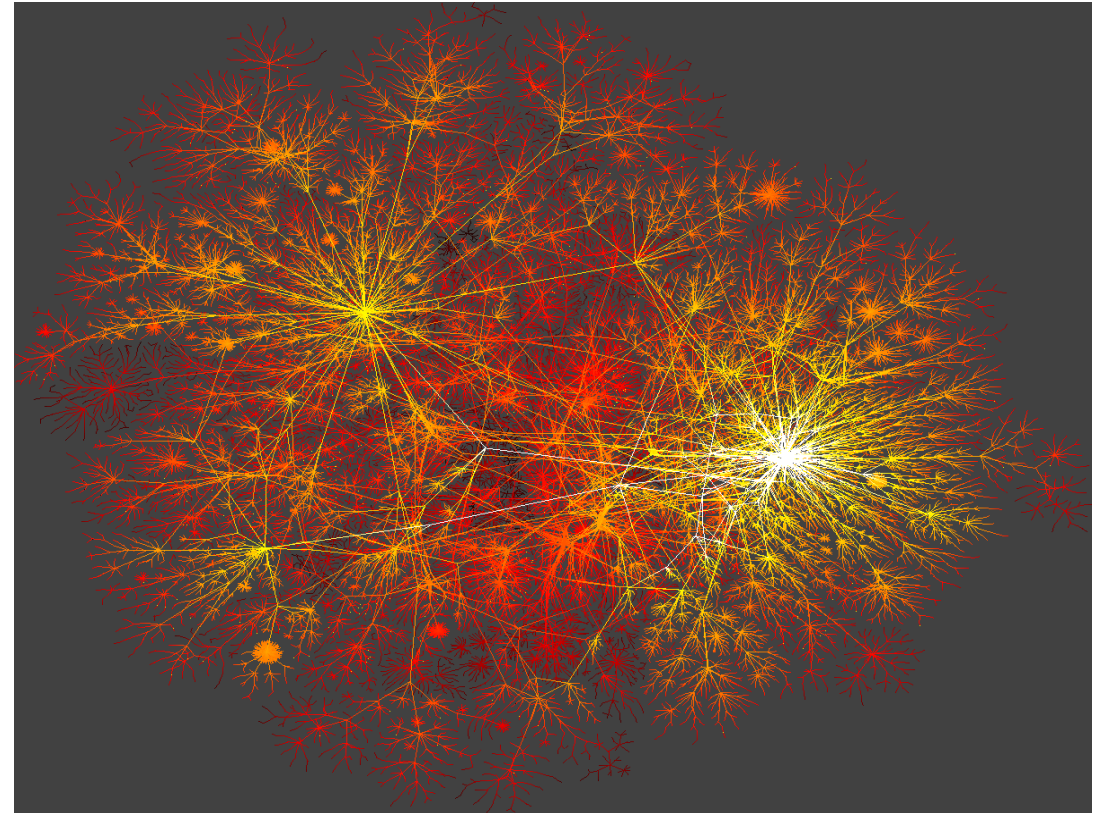
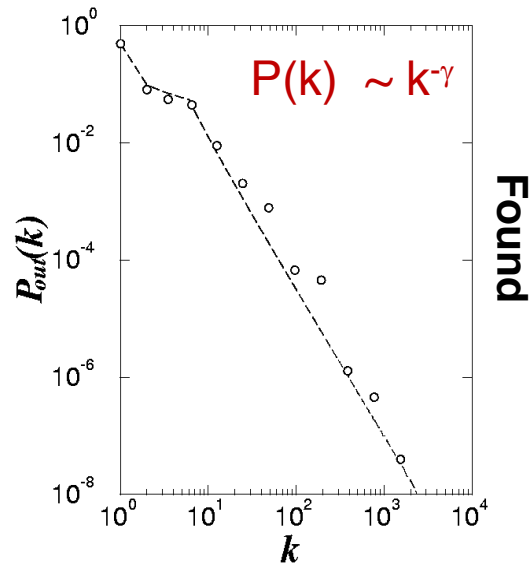
Real world Networks properties: Networks are Scale-free

Often the degree distribution follow a power law:

- Presence of few power-nodes (*hubs*)
- Average degree is not a representative indicator

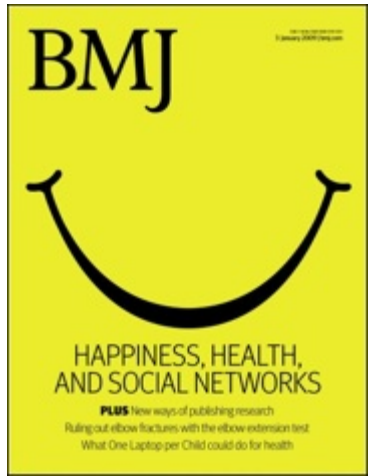
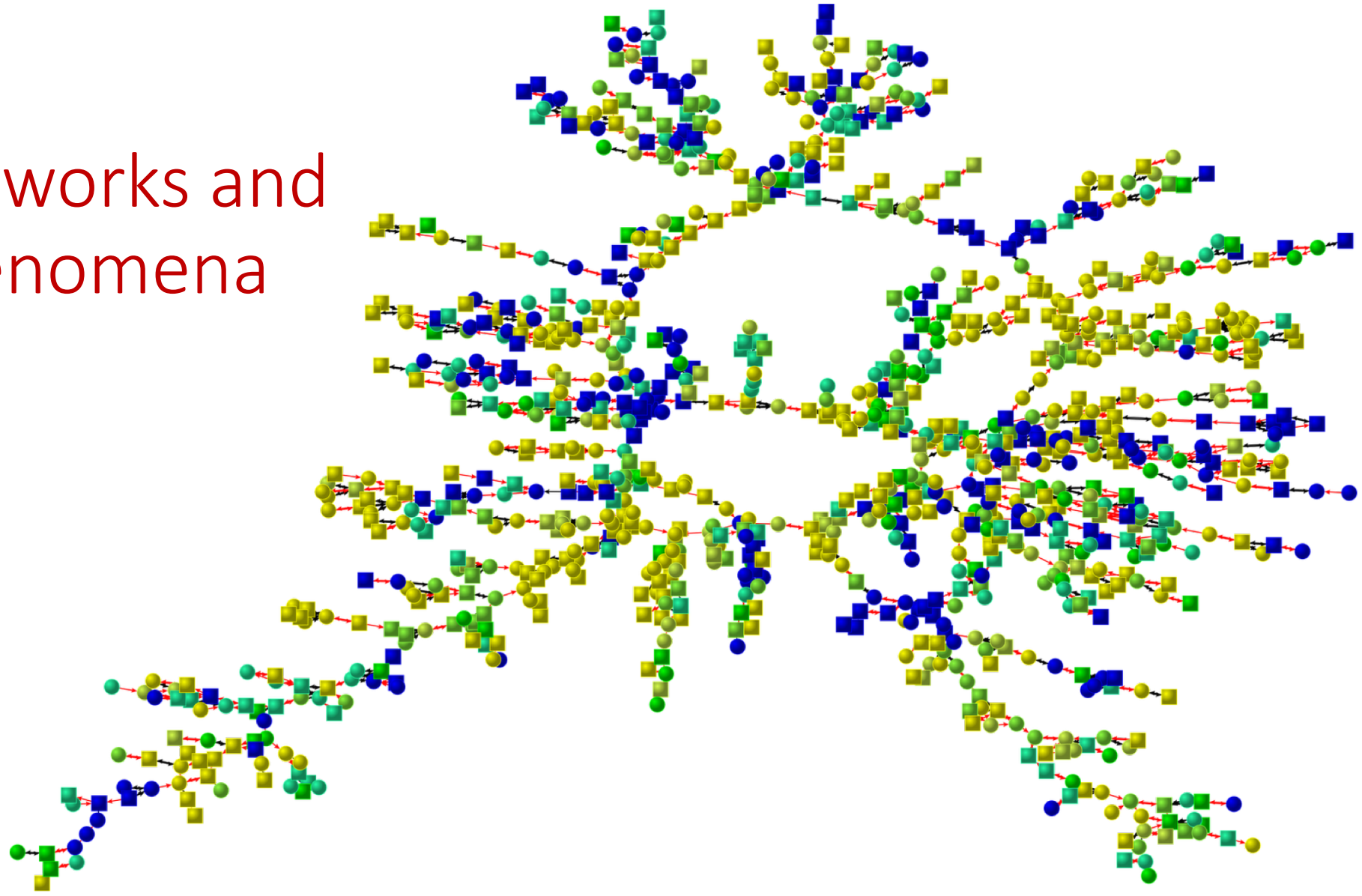


Expected



R. Albert, H. Jeong, A-L Barabasi, *Nature*, 401 130 (1999).

Complex Networks and Diffusive Phenomena



James H. Fowler, Nicholas A. Christakis.
Dynamic Spread of Happiness in a Large Social Network: Longitudinal Analysis Over 20 Years in the Framingham Heart Study
British Medical Journal 337 (4 December 2008)

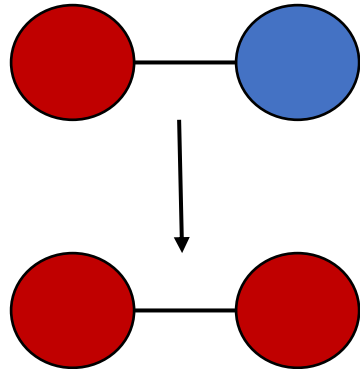
Breaking down a diffusion process

Diffusion *requires* network structure!

- It happens only when the carriers of the diseases/virus/idea are **connected to each other**.

Diffusive phenomena can modeled by describing:

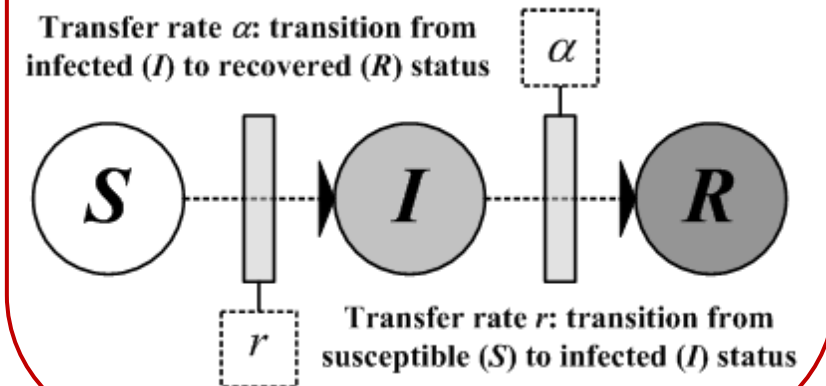
- “*node statuses*”
- “*transition rules*”



Example SIR model

Three node statuses:
(S)usceptible,
(I)nfected,
(R)ecovered

Two transition rules:
S->I;
I->R





A Network Diffusion Framework!

Simulate
Epidemics and
Opinion Dynamics
processes



Unfolding on top of
complex network structures

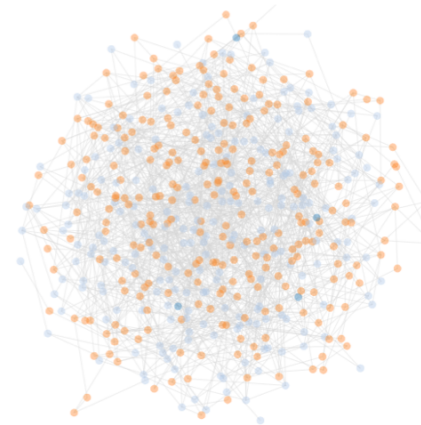
Network Diffusion Library

1. Network
nodes: 500 # edges: 1247

2. Models
SIR_0 SIR_1
Add model

3. Run iterations
Execute the model over the network
Which model(s) to use for the simulation?
All models
10
Run Iterations

Network Visualization



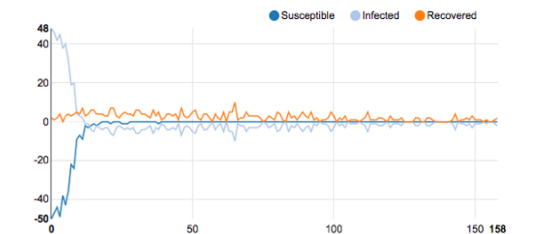
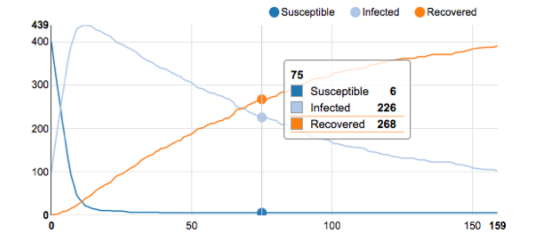
Model Statistics

Selected Model: SIR_0

beta: 0.1

gamma: 0.01

percentage_infected_nodes: 0.2



Programmatically
and **Visually!**

Available Models



Epidemics

(11 Models)

- SI / SIS / SIR
- SEIS / SEIR / SWIR
- Threshold / Profile / Profile-Threshold / Threshold-Blocked
- Independent Cascades

Opinion Dynamics

(6 Models)

- Majority Rule
- Voter / Q-Voter
- Sznajd
- Cognitive Opinion Dynamics
- Algorithmic Bias





A single workflow,
two type of users!

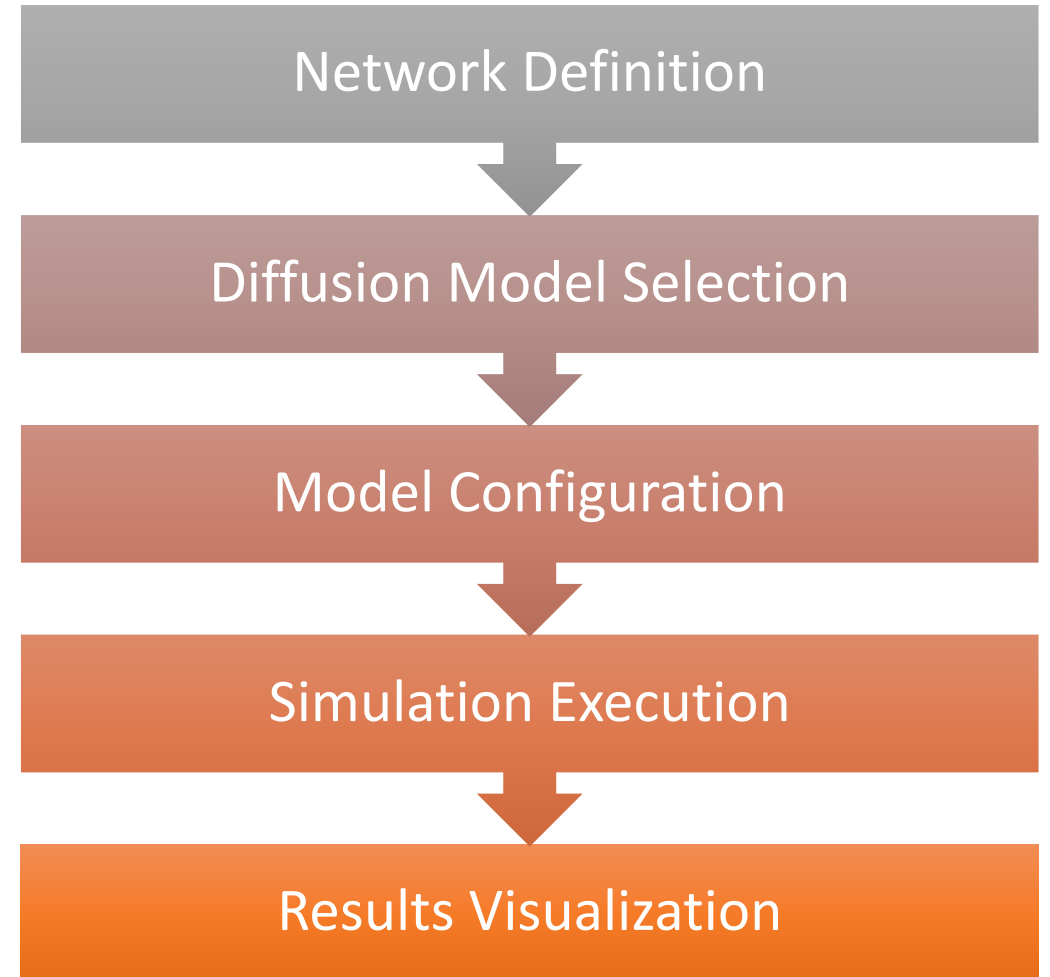
NDlib provide a common workflow to both programmers and analysts:

Programmers:

- Unified interface for several diffusion model
- Results Visualization facilities
- I/O standardization
- Extensibility

Analysts:

- Visual (web-based) platform
- Experiment configuration/execution
- Analytics as-a-service





Programmer: SIR Code Example

A simple, unified, interface:

- Load the Graph
- Select and configure the model
- Run the simulation

All models follow the same programmatic pattern and produce standardized results

```
import networkx as nx
import ndlib.models.ModelConfig as mc
import ndlib.models.epidemics.SIRModel as sir

# Network topology
g = nx.erdos_renyi_graph(1000, 0.1)

# Model selection
model = sir.SIRModel(g)

# Model Configuration
cfg = mc.Configuration()
cfg.add_model_parameter('beta', 0.01)
cfg.add_model_parameter('gamma', 0.005)
cfg.add_model_parameter("percentage_infected", 0.05)
model.set_initial_status(cfg)

# Simulation execution
iterations = model.iteration_bunch(200)
```



Programmer: Visual Analysis

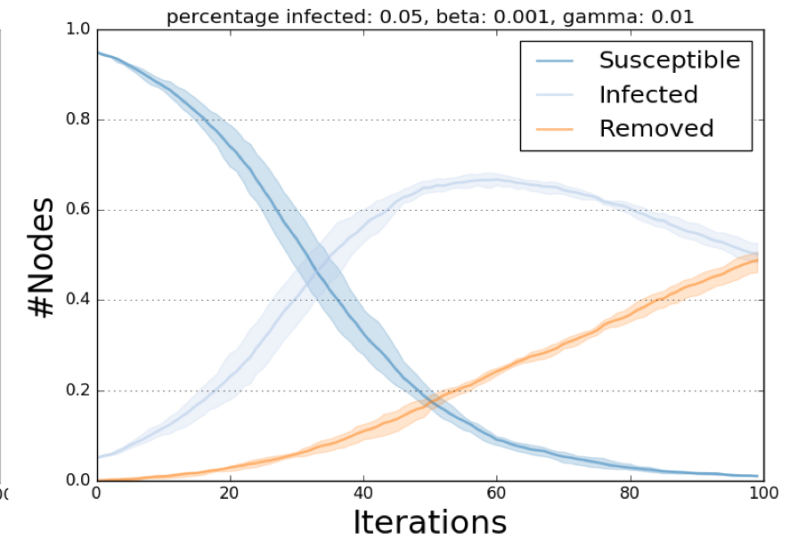
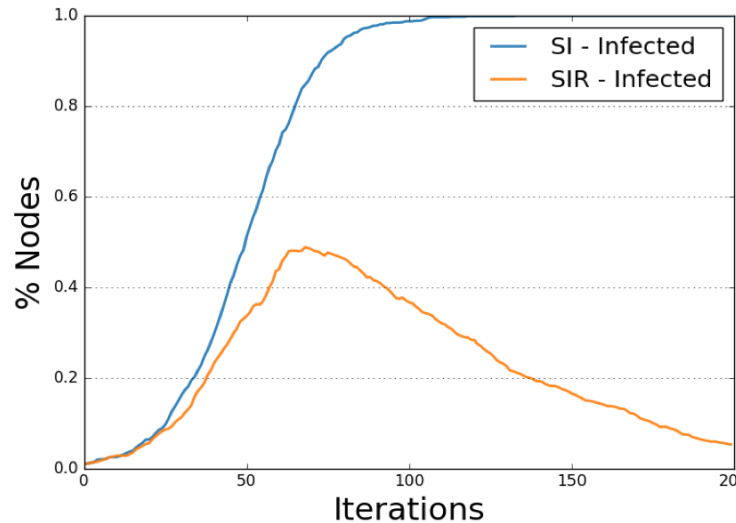
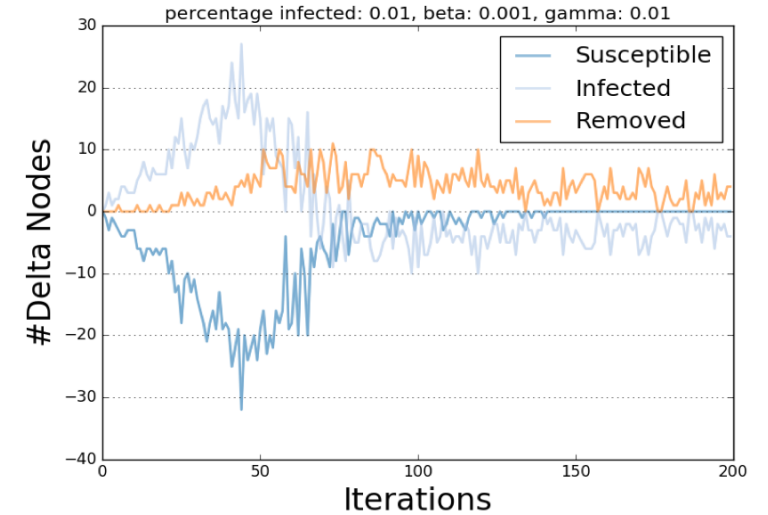
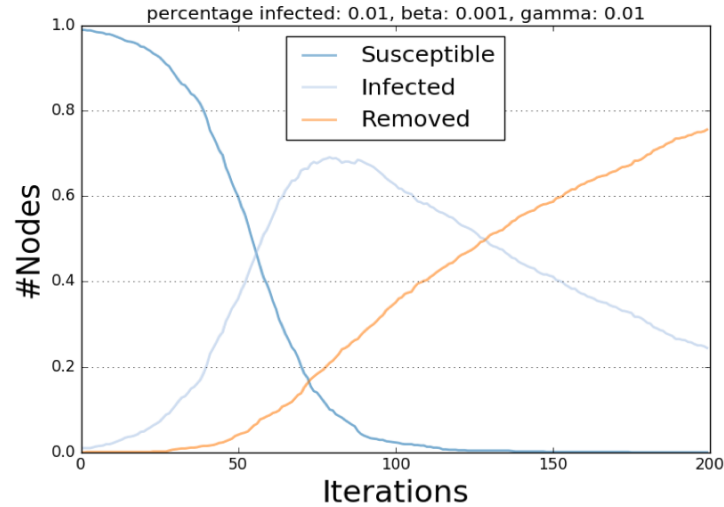
NDlib implements visualization facilities

Base Viz

- Diffusion Trends
- Prevalence

Advanced Viz

- Compare Models
- Multiple Run





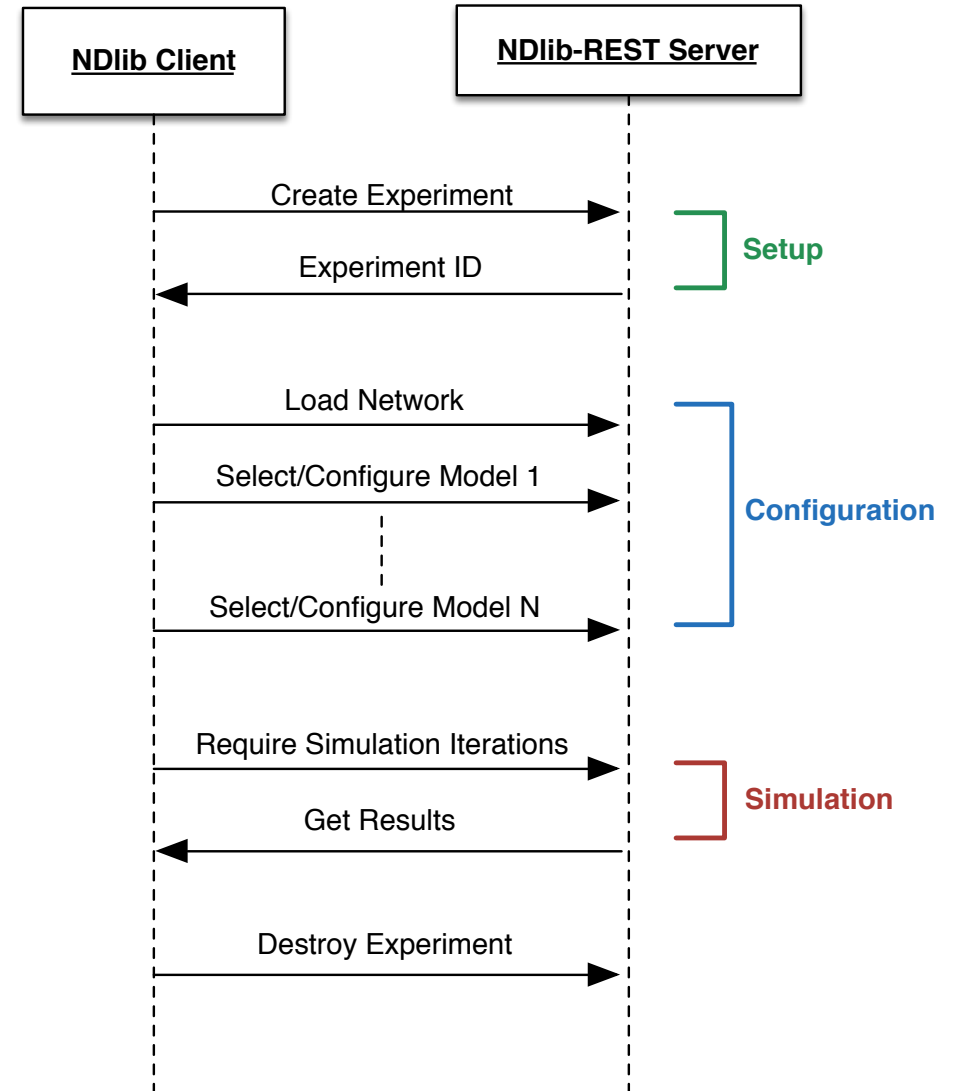
Programmer: Remote Experiments

NDlib offers a **remote experiment server** that, using a REST-full API, allows to:

- Create Ndlb experiments
- Configure them
- Execute them remotely

NDlib-REST aims to:

1. Decouple experiment definition/execution
2. Increase scalability





Analyst: Visual Simulation

Network Diffusion Library

1. Network

nodes: 500

edges: 1247

2. Models

SIR_0

SIR_1

Add model

3. Run iterations

Execute the model over the network

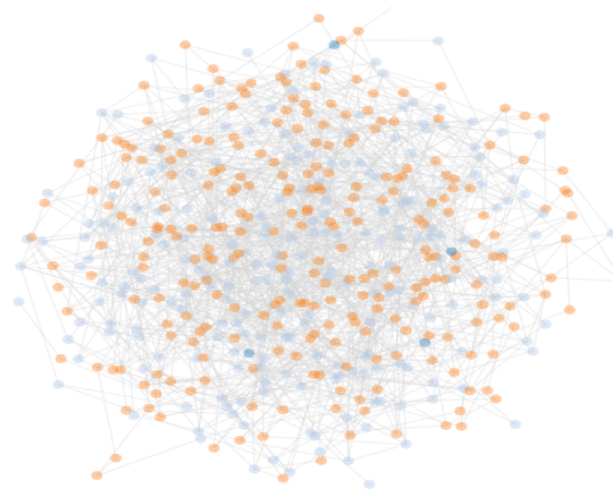
Which model(s) to use for the simulation?

All models

10

Run Iterations

Network Visualization



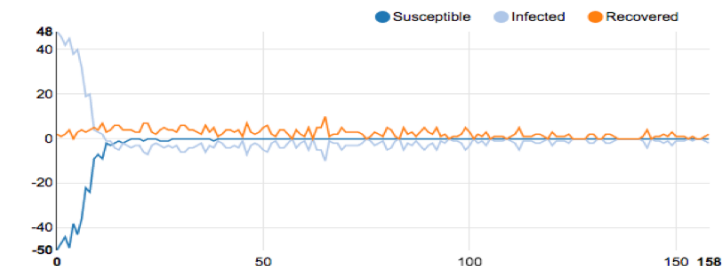
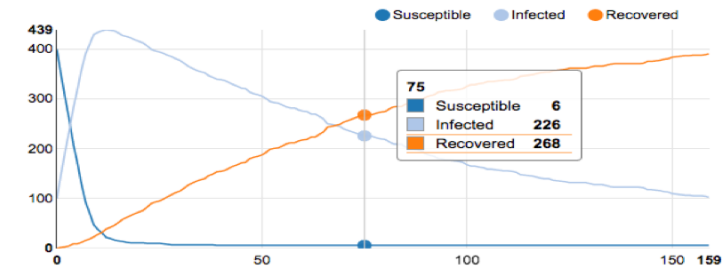
Model Statistics

Selected Model: SIR_0

beta: 0.1

gamma: 0.01

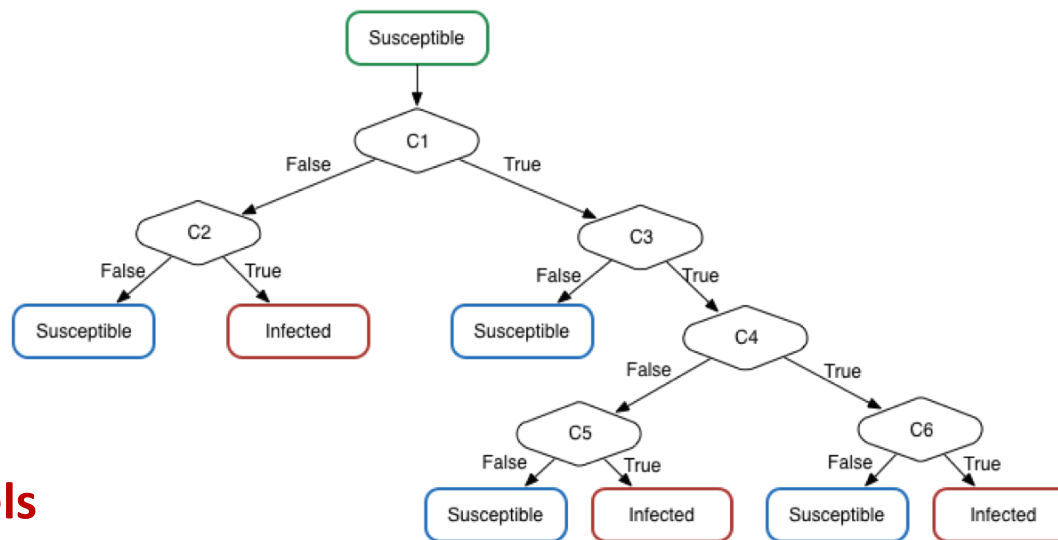
percentage_infected_nodes: 0.2



Ndlib 4.0: Advanced Features

Composite model definition

- Design diffusive models defining their transition rules as *trees* of atomic actions (compartments)

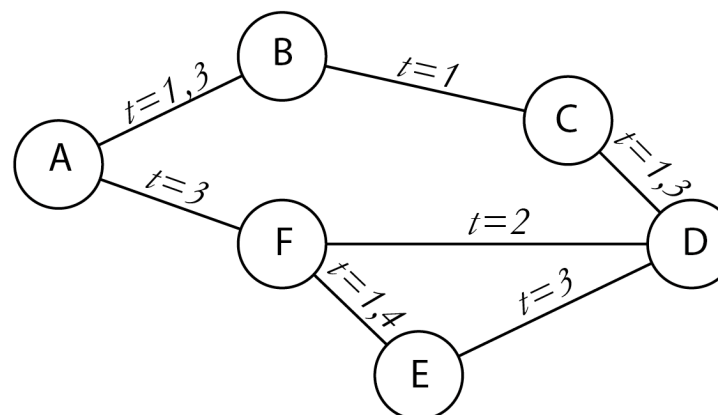


Support for Dynamic Network models

- Integration with DyNetX (ad-hoc library by CNR-UNIFI)

NDQL: Network Diffusion Query Language

- High-level query language for defining diffusion processes



```
CREATE_NETWORK g1
TYPE erdos_renyi_graph
PARAM n 300
PARAM p 0.1

MODEL SI

STATUS Susceptible
STATUS Infected

# Compartment definitions

COMPARTMENT c1
TYPE NodeStochastic
PARAM rate 0.1
TRIGGER Infected

# Rule definitions

RULE
FROM Susceptible
TO Infected
USING c1

# Model configuration

INITIALIZE
SET Infected 0.1

EXECUTE SI ON g1 FOR 100
```



State of art competitors analysis

Table 1 Diffusion libraries and tools. A checkmark indicates if the library is active.

Name	Lang.
NDLIB	Python
Epigrass	Python
GEMFsim	Python
Nepidemix	Python
EoN	Python
Epydemic	Python
ComplexNetworkSim	Python
Nxsim	Python
EpiModel	R
RECON	R
Sisspread	C
GLEaMviz	C++ Python

Table 2 Runtimes comparison. SIR model (parameters: $\beta = 0.001$, $\gamma = 0.01$), initial infected 5%, number of iterations 25, network model Barabasi–Albert graph. The compared libraries are organized by programming language

Library	Graph size (nodes)			
	10^3	10^4	10^5	10^6
NDLIB	0.060s	0.655s	7.554s	90.443s
ComplexNetworkSim	0.264s	3.152s	43.145s	576.072s
Nepidemix	0.283s	3.241s	43.190s	525.768s
EpiModel	0.025s	0.141s	2.289s	45.725s

on models, if any, natively implemented within

Net. Model	Active	License
NetworkX DyNetX	✓	BSD
NetworkX	✓	GPL
NetworkX	✓	-
NetworkX	✓	BSD
NetworkX	✓	MIT
NetworkX	✓	GPL
NetworkX		BSD
NetworkX		Apache
iGraph	✓	GPL
adhoc	✓	Various
adhoc	✓	GPL
adhoc	✓	SaaS



Publications

NDlib publications:

- **“NDlib: a Python Library to Model and Analyze Diffusion Processes Over Complex Networks”**
G. Rossetti, L. Milli, S. Rinzivillo, A. Sirbu, D. Pedreschi, F. Giannotti. International Journal of Data Science and Analytics. 2017. [DOI:0.1007/s41060-017-0086-6](https://doi.org/10.1007/s41060-017-0086-6)
- **“NDlib: Studying Network Diffusion Dynamics”**
G. Rossetti, L. Milli, S. Rinzivillo, A. Sirbu, D. Pedreschi, F. Giannotti. IEEE International Conference on Data Science and Advanced Analytics, DSAA. 2017.
- **“NDlib: A Python Library to model and analyze diffusion processes over complex networks”**
G. Rossetti, L. Milli, S. Rinzivillo. Demo @ The Web Conference, WWW, 2018.

Publications using NDlib:

- **“Information Diffusion in Complex Networks: The Active/Passive Conundrum”**
L. Milli, G. Rossetti, D. Pedreschi, F. Giannotti International Conference on Complex Networks and their Applications, 2017. [DOI:10.1007/978-3-319-72150-7_25](https://doi.org/10.1007/978-3-319-72150-7_25)
- **“Diffusive Phenomena in Dynamic Networks: a data-driven study”**
L. Milli, G. Rossetti, D. Pedreschi, F. Giannotti. 9th Conference on Complex Networks, CompleNet, 2018.



When:

Right now, NDlib v4.0.1 is out!



Where:

- Pypi: <https://pypi.python.org/pypi/ndlib>
- GitHub NDlib: <https://github.com/GiulioRossetti/ndlib>
- GitHub NDlib-REST: <https://github.com/GiulioRossetti/ndlib-rest>
- Documentation: <http://ndlib.readthedocs.io/>
- SoBigData: <http://www.sobigdata.eu>



Who:

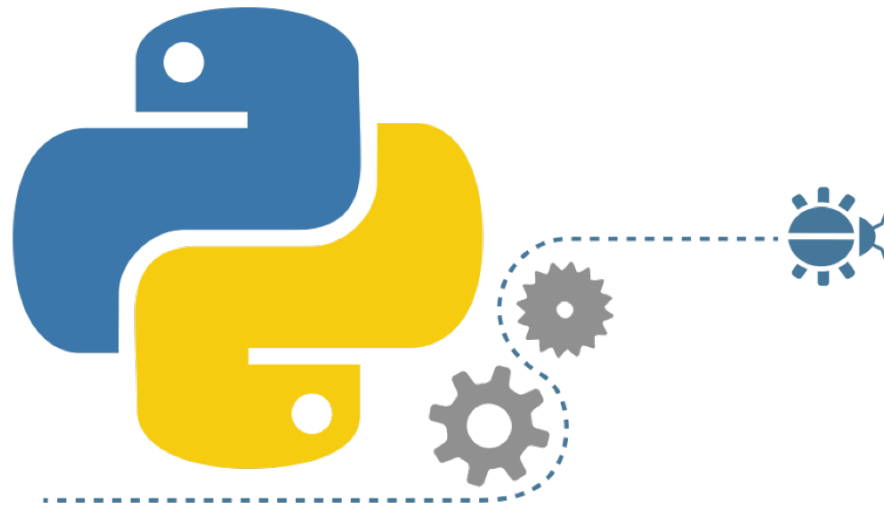




Demo/Tutorial

How many people here know a **programming language**?

How many people here have used **Python**?





Where to start...

Install **Anaconda**
(Python 3 version!)

<https://www.anaconda.com/download/>

Anaconda is a python distribution for data scientists.

It provides out-of-the box support for:

- Data modeling
- Analysis
- Visualisation
- ...



ANACONDA
Powered by **Continuum Analytics**®

NDlib tutorial:

<https://goo.gl/oGkuyk>

NDlib-viz (testing server):

<http://sobigdatata2.isti.cnr.it/NDLibViz/>

Library Documentation:

<http://ndlib.readthedocs.io/>

