Recurrent Neural Networks

JPMorgan Chase & Co.

Bruno Gonçalves

www.bgoncalves.com github.com/bmtgoncalves/RNN



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The views and opinions expressed in this article are those of the authors and do not necessarily reflect the official policy or position of my employer. The examples provided with this tutorial were chosen for their didactic value and are not mean to be representative of my day to day work.

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References













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- "neurons that fire together wire together" (Hebb)
- Different areas perform different functions using same structure (Modularity)

















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 - The optimization algorithm.





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 - The constraints Neural Network
 - The function to optimize
 Prediction Error
 - The optimization algorithm. Gradient Descent







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http://github.com/bmtgoncalves/Neural-Networks



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Non-Linear function



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• Compute new sets of features



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- Non-Linear function
- Differentiable
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- Compute new sets of features
- Each layer builds up a more abstract
 representation of the data



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Activation Function - Sigmoid

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But how can we propagate back the errors and update the weights?
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 - Update the weights
- The error at the output is a weighted average difference between predicted output and the observed one.
- For inner layers there is no "real output"!



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The Cross Entropy is complementary to sigmoid activation in the output layer and improves its stability.

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• Find the gradient for each training batch

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- Take a step **downhill** along the direction of the gradient

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- Repeat until "convergence".



INPUT TERMS

FEATURES PREDICTIONS ATTRIBUTES PREDICTABLE VARIABLES

MACHINE

ALGORITHMS TECHNIQUES MODELS

OUTPUT TERMS

CLASSES RESPONSES TARGETS DEPENDANT VARIABLES

Feed Forward Networks



$$h_t = f\left(x_t\right)$$

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Recurrent Neural Network (RNN)



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• Each output depends (implicitly) on all previous outputs.



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- Each output depends (implicitly) on all previous outputs.
- Input sequences generate output sequences (seq2seq)



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• What if we want to keep explicit information about previous states (memory)?



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- How much information is kept, can be controlled through gates.
- LSTMs were first introduced in 1997 by Hochreiter and Schmidhuber



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1 minus the input

_ong-Short Term Memory (LSTM)





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Element wise addition







1 minus the input

Long-Short Term Memory (LSTM)











1 minus the input

Long-Short Term Memory (LSTM)



















Neural Networks?



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• Language Modeling and Prediction



- Language Modeling and Prediction
- Speech Recognition



- Language Modeling and Prediction
- Speech Recognition
- Machine Translation



- Language Modeling and Prediction
- Speech Recognition
- Machine Translation
- Part-of-Speech Tagging



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- Language Modeling and Prediction
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- Machine Translation
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- Sentiment Analysis
- Summarization
- Time series forecasting

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Gated Recurrent Unit (GRU)

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- Can be considered as a simplification of LSTMs
- Similar performance to LSTM in some applications, better performance for smaller datasets.





Element wise multiplication



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Gated Recurrent Unit (GRU)



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Element wise multiplication



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Using a running window of a certain length

• Supervised learning model

Input Sequence	output
Mary had a little	lamb
had a little lamb	whose
a little lamb whose	fleece
little lamb whose fleece	was
lamb whose fleece was	white
whose fleece was white	as
fleece was white as	SNOW





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Open Source neural network library written in Python



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- Implements Layers, Objective/Loss functions, Activation functions, Optimizers, etc...





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Keras

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 - LSTM(units, input_shape, activation='tanh', use_bias=True, dropout=0.0, return_sequences=False)

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- model.summary() Output a textual representation of the model

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