JPMorgan Chase \& Co.

## Recurrent Neural Networks

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## Disclaimer

The views and opinions expressed in this article are those of the authors and do not necessarily reflect the official policy or position of my employer. The examples provided with this tutorial were chosen for their didactic value and are not mean to be representative of my day to day work.

## References



## How the Brain "Works" (Cartoon version)



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- Weights adapt during the learning process
- "neurons that fire together wire together" (Hebb)
- Different areas perform different functions using same structure (Modularity)



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- The optimization algorithm. Gradient Descent



## Artificial Neuron

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Inputs

## Artificial Neuron



Inputs Weights

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## Activation Function - Sigmoid

Sigmoid activation function


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- non-decreasing
- Compute new sets of features
- Each layer builds up a more abstract representation of the data
- Perhaps the most common

Sigmoid activation function


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- But how can we propagate back the errors and update the weights?


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- Forward propagate the inputs and calculate the deltas
- Update the weights
- The error at the output is a weighted average difference between predicted output and the observed one.
- For inner layers there is no "real output"!


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- Cross Entropy

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J=-\frac{1}{N} \sum_{n}\left[y_{n}^{T} \log a_{n}+\left(1-y_{n}\right)^{T} \log \left(1-a_{n}\right)\right]
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> The Cross Entropy is complementary to sigmoid activation in the output layer and improves its stability.

## Gradient Descent


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## Gradient Descent



- Find the gradient for each training batch


## Gradient Descent



- Find the gradient for each training batch
- Take a step downhill along the direction of the gradient

$$
\theta_{m n} \leftarrow \theta_{m n}-\alpha \frac{\partial H}{\partial \theta_{m n}}
$$

## Gradient Descent



## Gradient Descent



## INPUT TERMS

FEATURES
PREDICTIONS
ATTRIBUTES
PREDICTABLE VARIABLES

## MACHINE

## ALGORITHMS

TECHNIQUES
MODELS

## OUTPUT TERMS

CLASSES
RESPONSES
TARGETS
DEPENDANT VARIABLES

## Feed Forward Networks



$$
h_{t}=f\left(x_{t}\right)
$$

## Feed Forward Networks



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$$
h_{t}=f\left(x_{t}, h_{t-1}\right)
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- Each output depends (implicitly) on all previous outputs.



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- Each output depends (implicitly) on all previous outputs.
- Input sequences generate output sequences (seq2seq)



## Recurrent Neural Network (RNN)


$h_{t}=\tanh \left(W h_{t-1}+U x_{t}\right)$

## Recurrent Neural Network (RNN)



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& \text { concatenate } \\
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- How much information is kept, can be controlled through gates,
- LSTMS were first introduced in 1997 by Hochreiter and Schmidhuber



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\begin{array}{ll}
f=\sigma\left(W_{f} h_{t-1}+U_{f} x_{t}\right) & g=\tanh \left(W_{g} h_{t-1}+U_{g} x_{t}\right) \\
i=\sigma\left(W_{i} h_{t-1}+U_{i} x_{t}\right) & c_{t}=\left(c_{t-1} \otimes f\right)+(g \otimes i) \\
o=\sigma\left(W_{o} h_{t-1}+U_{o} x_{t}\right) & h_{t}=\tanh \left(c_{t}\right) \otimes o
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## Neural Networks?



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## Applications

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- Language Modeling and Prediction


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- Introduced in 2014 by Cho
- Meant to solve the Vanishing Gradient Problem
- Can be considered as a simplification of LSTMs
- Similar performance to LSTM in some applications, better performance for smaller datasets.

$z=\sigma\left(W_{z} h_{t-1}+U_{z} x_{t}\right) \quad c=\tanh \left(W_{c}\left(h_{t-1} \otimes r\right)+U_{c} x_{t}\right)$
$r=\sigma\left(W_{r} h_{t-1}+U_{r} x_{t}\right) \quad h_{t}=(z \otimes c)+\left((1-z) \otimes h_{t-1}\right)$
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- Can be formulated as find the next word:

My name is ___
The sky is $\qquad$ $-$
$P($ Bruno $\mid m y$, name, is $) \gg P($ red $\mid m y$, name, is $)$
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\begin{aligned}
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- So given a piece of text, we build a training dataset:

Mary had a little lamb whose fleece was white as snow.
Using a running window of a certain length

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Using a running window of a certain length

- Supervised learning model
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Input Sequence
Mary had a little
, had a little lamb whose a little lamb whose fleece little lamb whose fleece was lamb whose fleece was white whose fleece was white fleece was white as

## Or legos?



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- Implements Layers, Objective/Loss functions, Activation functions, Optimizers, etc...
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- loss - 'mean_squared_error', 'categorical_crossentropy', ‘kulllback_leibler_divergence’, etc...


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- model.summary() - Output a textual representation of the model
github.com/bmtgoncalves/RNN

