

Market Liquidity, Funding Liquidity, and TED Spread: A Two-Regime Model

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Liquidity

- *Liquidity* is a key idea in markets:
 - *Market liquidity*: ease of trading an asset without moving price.
 - *Funding liquidity*: ease of obtaining funds (usu. w/collateral).
- These different liquidities are endogenous:
 - Funding for intermediaries, investors affects market liquidity.
 - Market liquidity improves value of funding collateral.
- Theory: two equilibria (spirals) for market, funding liquidity.
 - Peacetime: one liquidity decreases \implies other increases
 - Crises: one liquidity decreases \implies other decreases
- Theory and evidence for bad equilibrium in recent crisis.
- Few empirical studies of interaction b/w these liquidities.

How Market Liquidity Affects Funding Liquidity

- Question: how does market liquidity affect funding liquidity?
- Find a proxy for equity-collateralized funding liquidity; and,
- Use that to study funding, market liquidity in equity markets.
- Lets us test important features of the theorized relation:
 - Two regimes (stabilizing vs destabilizing)
 - Feedback b/w funding liquidity vs market liquidity, volatility

Results Preview

- Data \implies two regimes in funding, market liquidity dynamics.
- May separate regimes using a TED spread threshold: 48 bp.
- TED spread $\leq 48\text{bp}$ \implies stabilizing funding cycle:
 - Bid-ask spreads $\uparrow 10\%$ \implies funding illiquidity $\downarrow 25\%–36\%$.
 - First empirical verification of stabilizing cycle.
- TED spread $> 48\text{bp}$ \implies destabilizing funding cycle:
 - Bid-ask spreads $\uparrow 10\%$ \implies funding illiquidity $\uparrow 16\%–26\%$?
- Handling endogeneity: crucial to analyzing funding cycles.

Related Literature

- Theory: Funding Liquidity \iff Market Liquidity
 - Sophisticated investors/arbitrageurs supply market liquidity.
 - Must finance positions, usu. by collateralized lending.
 - Pay loan fees/margins, budget constrained in crises.
 - So expect to see two regimes of liquidity provision.
 - Gromb and Vayanos (2002, 2010)
 - Brunnermeier and Pedersen (2009)
- Empirical Studies
 - Funding Liquidity \implies Market Liquidity
 - Mitchel, Pedersen and Pulvino (2009)
 - Comerton-Forde et al. (2010)
 - Funding Liquidity \longleftarrow Market Liquidity
 - Drehmann and Nikolaou (2013)
 - Does not account for endogeneity, two regimes.

Theory of Market, Funding Liquidity: Destabilizing

Theory for destabilizing market, funding liquidity interactions:

- Cost of collateralized borrowing: increases w/asset volatility.
- Drop in market liquidity may increase borrowing costs
 - Financiers don't know fundamental value of assets, and
 - Worry about lower liquidity of collateral, increase loan fees.
 - Budget constraint binds, unwinding positions moves prices
 - Prices further from fundamentals, market liquidity ↓
 - \implies **Destabilizing Funding Cycle**
- Destabilizing funding \implies flight-to-quality.

Theory of Market, Funding Liquidity: Stabilizing

Theory for stabilizing market, funding liquidity interactions:

- Drop in market liquidity may decrease borrowing costs
 - Financiers believe prices will return to fundamental value,
 - \implies arb positions more profitable, decrease loan fees
 - Budget constraint relaxes, positions grow moving prices
 - Prices move closer to fundamentals, market liquidity \uparrow
 - \implies **Stabilizing Funding Cycle**
- Agrees with most ideas on self-healing nature of markets.

Funding Liquidity: Equity-Collateralized Loans

- Best measure of collateralized funding: repo rates.
- Unfortunately, we could not find good repo rates source.
- However, believe stock loan data is a good proxy:
 - Traders borrow stock (usu for shorting) via stock loans.
 - Fees increase when more demand to borrow.
 - Lender also holds back *haircut* of deposited cash.
 - Haircut, fees rise when stock more likely to decline.
 - Thus haircut, fees proxy for perceived collateral quality.
- Loan fee data available; haircut data not (but correlated).

Stock Loan Fees

- Consider demand for borrowing stock (usually: to short)
 - Curve shift out/in \implies more/less capital betting on price fall
- Cohen, Diether, and Malloy (2007) studied stock loan fees.
 - Isolated outward shifts of stock loan demand curves
 - \implies Significant negative abnormal next-month returns
 - \implies Stock loans reveal private information about stock
- Demand curve shifts in/out: stock is worse/better collateral.
- Use daily S&P 500 stock loan data, 200607–201105⁴:
 - Volume-Weighted Average stock loan Fee (VWAF)
 - Total Balance Quantities (TBQ) = qty of stock on loan
 - # loan transactions: stock i , day t ($Trades_{it}$)

⁴We thank Data Explorers for these data.

Funding Illiquidity: Average Stock Loan Fees

- Isolate shifts in stock loan (shorting) demand curve:

$$\mathbb{1}_{DS,it} = \begin{cases} 1 & \Delta VWAF_{i,t} > 0 \cap \Delta TBQ_{i,t} > 0; \\ 1 & \Delta VWAF_{i,t} < 0 \cap \Delta TBQ_{i,t} < 0; \\ 0 & \text{else.} \end{cases} \quad (1)$$

- Measure of funding illiquidity, $fundilliq_t$:

$$fundilliq_t = \log \left(\frac{\sum_{i=1}^N Trades_{it} \times VWAF_{it} \times \mathbb{1}_{DS,it}}{\sum_{i=1}^N Trades_{it} \times \mathbb{1}_{DS,it}} \right). \quad (2)$$

Funding Illiquidity: Plot

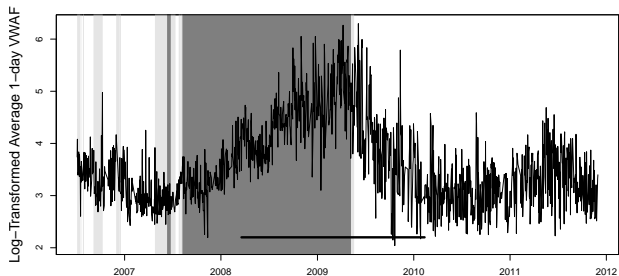


Figure: $\text{Log}(\text{Trade-Weighted Average Fee on S\&P 500 Stock Loans})$.
Light gray: $\text{ted}_t > 50\text{bp}$; dark gray: $\text{ted}_t > 80\text{bp}$; black bar: PDCF
(03/2008–02/2010)

Market Illiquidity: Bid-Ask Spreads

- Market illiquidity: Mean % bid-ask spreads of S&P 500 stocks
- N.B. From CBOE calculation, changed in late-May 2011.⁵
- Take logarithm to reduce influence of skewness

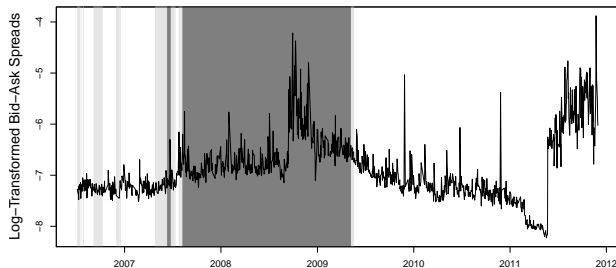


Figure: Log(Bid-Ask Spread for S&P 500 Stocks). Light gray: $ted_t > 50bp$; dark gray: $ted_t > 80bp$

⁵This change limits our ability to extend the study.

Volatility

- Market volatility proxy: CBOE Implied Volatility Index (VIX)

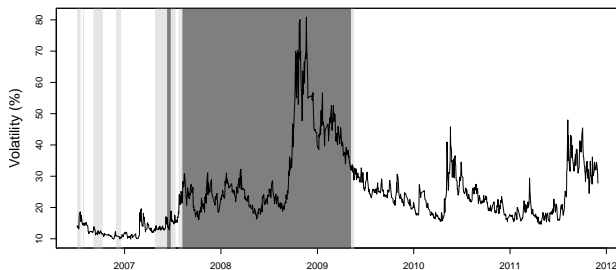


Figure: CBOE Implied Volatility Index. Light gray: $ted_t > 50\text{bp}$; dark gray: $ted_t > 80\text{bp}$

TED Spread

- TED Spread: Treasury vs EuroDollar Deposits
- Spread between LIBOR and 3M US T-bill rates
- Used to separate stabilizing, destabilizing funding regimes

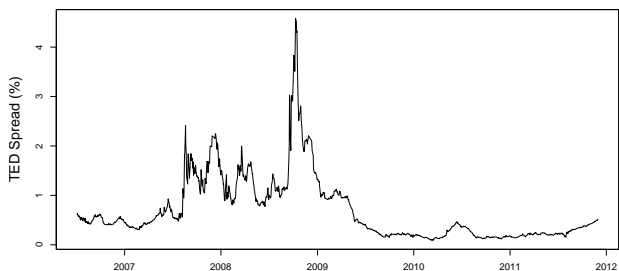


Figure: TED Spread. lower dashed line: $ted_t > 50\text{bp}$; upper dashed line: $ted_t > 80\text{bp}$

Instruments

- 1 Inter-trade duration trend: driven by exogenous tech shocks
 - Trade activity \implies mkt liquidity (George and Longstaff, 1993)
- 2 AAA liquidity: $aaaliq = \Delta y_{AAA} - \Delta LIBOR$
 - Bond liquidity \implies stock liquidity: Chordia, Sarkar, Subrahmanyam (2005)
 - Change in AAA yields due to bond (il)liquidity
 - Exogenous to credit risk which affects stock loan fees
- 3 Lagged volatility: 'internal' instrument for stock volatility cf Bloom et al. (2007)

Instrument: Inter-trade Duration Trend

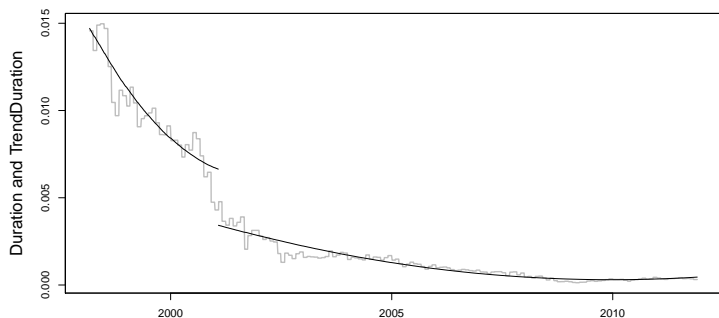


Figure: Inter-trade Duration Trend for US stocks (in years). Gray line: inter-trade duration; black line: trend pre-/post-NYSE decimalization in Jan 2001

Instrument: AAA Liquidity

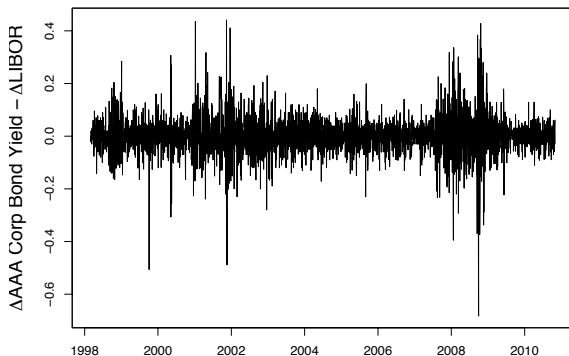


Figure: Difference b/w Δ Yields(1Y AAA Corporates), Δ LIBOR: Mar 1998–Dec 2011

Two-Regime Specification

- Allow for regime change if credit spread crosses threshold κ .
- Define market stress indicator, specify linear threshold model:

$$stress_t(\kappa) = \begin{cases} 1 & ted_t > \kappa \\ 0 & \text{else} \end{cases} \quad (3)$$

$$\begin{aligned} fundilliq_t = & \beta_0 + \beta_1 mktilliq_t + \beta_2 vol_t + \beta_3 volsq_t \\ & + \beta_4 ted_t + \beta_5 stressmktilliq_t + \beta_6 stressvol_t \\ & + \beta_7 stressted_t + \varepsilon_t \end{aligned} \quad (4)$$

where *stress* variables have interaction with $stress_t(\kappa)$.

- Estimation via Hansen (2000), Caner and Hansen (2004).
- For threshold $\hat{\kappa}$, estimate other coefficients by 2SLS.

First-Stage Regressions

- First-stage regressions for linear, two-regime IV.
- *durtrend*: less trading = less liquid, less volatile markets.
 - Agrees with George and Longstaff (1993).
 - Except $ted > 48bp$: less trading *increases* mkt liquidity.
 - Perhaps reduces panic trading?
- *aaaliq*: bond illiquidity $\uparrow \implies$ equity illiquidity \downarrow .
 - Agrees w/Chordia, Sarkar, Subrahmanyam (2005).
 - However, less effect when $ted > 48bp$.
- *F*-tests indicate relevance of instruments at 99% level

Second-Stage: Funding Liquidity vs Market Liquidity

Covariates	Linear Model		Two-Regime Model	
	OLS	IV	OLS	IV
<i>(intercept)</i>	4.732 (0.516)	8.399 (2.746)	2.594 (0.665)	-26.327 (18.332)
<i>mktilliq_t</i>	0.323 (0.065)	0.790 (0.348)	0.014 (0.082)	-3.612 (2.283)
<i>vol_t</i>	6.263 (0.655)	4.953 (1.290)	5.192 (0.652)	13.093 (7.240)
<i>volsq_t</i>	-4.550 (0.894)	-3.627 (1.206)	-8.303 (0.924)	-6.818 (6.712)
<i>ted_t</i>	0.012 (0.042)	-0.174 (0.134)	0.717 (0.292)	3.965 (1.962)
<i>stress_t</i>			2.466 (0.977)	40.553 (13.222)
<i>stressmktilliq_t</i>			0.382 (0.124)	5.210 (1.685)
<i>stressvol_t</i>			4.824 (0.649)	-6.267 (4.853)
<i>stressed_t</i>			-1.055 (0.296)	-4.599 (1.617)
Threshold κ			0.43 [0.42, 0.44]	0.48 [0.44, 0.49]

Second-Stage Regression Results: Commentary

- Relationship b/w funding, market liquidity has two regimes:
 - ① Stable markets ($ted \leq 48bp$): significant at 90% level.
 - Bid-ask spreads $\uparrow 10\% \implies$ funding illiquidity $\downarrow 36\%$.
 - \implies stabilizing funding cycle.
 - ② Unstable markets ($ted > 48bp$): not significant
 - Bid-ask spreads $\uparrow 10\% \overset{?}{\implies}$ funding illiquidity $\uparrow 16\%$.
 - Weak evidence of destabilizing funding cycle.
- Volatility $\uparrow \implies$ funding illiquidity \uparrow . (stronger in peacetime)
- Results are likely stronger: IV 2SLS inflates std errors.
- Naive approaches miss liquidity, volatility significance.
 - Signs off, magnitudes much smaller.

Robustness: Adding an Autoregressive Term

Covariates	Linear Model		Two-Regime Model	
	OLS	IV	OLS	IV
<i>(intercept)</i>	1.953 (0.193)	<i>-0.111</i> (0.061)	<i>1.574</i> (0.581)	<i>-19.440</i> (14.204)
<i>mktilliq_t</i>	0.129 (0.003)	<i>-0.014</i> (0.008)	<i>0.024</i> (0.070)	<i>-2.573</i> (1.747)
<i>fundilliqt-1</i>	0.574 (0.001)	1.002 (0.001)	0.449 (0.037)	<i>0.528</i> (0.071)
<i>vol_t</i>	2.665 (0.313)	<i>0.021</i> (0.026)	<i>2.585</i> (0.574)	<i>8.887</i> (5.221)
<i>volsq_t</i>	-1.918 (0.539)	<i>-0.009</i> (0.025)	-3.893 (0.858)	<i>-4.804</i> (3.721)
<i>ted_t</i>	0.010 (0.001)	<i>0.005</i> (0.003)	<i>0.382</i> (0.239)	<i>2.669</i> (1.532)
<i>stress_t</i>			<i>0.312</i> (0.879)	<i>20.706</i> (8.448)
<i>stressmktilliq_t</i>			<i>0.107</i> (0.108)	<i>2.631</i> (1.086)
<i>stressfundilliqt-1</i>			<i>0.107</i> (0.051)	<i>0.010</i> (0.074)
<i>stressvol_t</i>			<i>2.109</i> (0.600)	<i>3.169</i> (2.554)
<i>stressed_t</i>			<i>-0.523</i> (0.243)	<i>-2.809</i> (1.171)
Threshold κ			0.44 [0.21, 0.47]	0.48 [0.46, 0.49]

Robustness Check: Autoregressive Term

- Relationship b/w funding, market liquidity again two regimes:
 - ① Stable markets ($ted \leq 48bp$): not significant but right sign.
 - Bid-ask spreads $\uparrow 10\% \implies$ funding illiquidity $\downarrow 25\%$.
 - weak evidence of stabilizing funding cycle.
 - ② Unstable markets ($ted > 48bp$): significant at 90% level.
 - Bid-ask spreads $\uparrow 10\% \xrightarrow{?} \implies$ funding illiquidity $\uparrow 26\%$.
 - \implies destabilizing funding cycle.
- Volatility $\uparrow \implies$ funding illiquidity \uparrow . (stronger in crisis?)
- Threshold again 48 bp.
- Naive approaches miss liquidity, volatility significance.
 - Signs off and/or magnitudes much smaller.

Robustness Check: Stock Loan Data

- Look at full/filtered size-weighted stock loan data.
- Look at shifts in demand curve or all shifts.
- Weight average fees by loan sizes, not by # loans.
- These changes expose us to more noise, outliers.
- Find significant threshold of 47 bp (vs 48 bp) in both cases.
- However, coefficients not significant in either case.

Robustness Check: Another Funding Measure

- Second check: another funding measure (Broker Call Rate).
- Charged by commercial banks to broker-dealers.
 - Rate is charged on short-term margin loans
 - Problem #1: rate is rarely-changing spread over Fed Funds.
 - Problem #2: No information on volume transacted.
- Modeled spread over 3M US T-bills; may need to be changed.
- Find two regimes, TED spread threshold of 77 bp:
 - $ted < 77bp$: market illiquidity $\uparrow 10\%$ $\implies fundilliq \downarrow 3\%$
 \implies stabilizing funding cycle
 - $ted \geq 77bp$: stabilizing cycle is weakened.
 \implies no destabilizing relationship
- Sensible: don't expect policy-makers to destabilize market.
- Need more work to decide if measure is useful/informative.

Conclusion

- Introduce stock-loan proxy for equity-collateralized funding.
- Use a two-regime 2SLS estimation to reveal:
 - Relationship b/w funding, market liquidity has two regimes.
 - May separate regimes using a TED-spread threshold.
 - Improper estimation cannot detect these funding cycles.
- Stable markets ($ted \leq 48bp$):
 - Bid-ask spread $\uparrow 10\% \implies$ funding illiquidity $\downarrow 25\%–36\%$.
 - Stabilizing funding cycle arises. (First evidence!)
- Unstable markets ($ted > 48bp$):
 - Bid-ask spread $\uparrow 10\% \implies$ funding illiquidity $\uparrow 16\%–26\%$.
 - Destabilizing funding cycle arises.
- Funding liquidity based on volatility.
- Two regimes may exist in other funding measures.